

Competing with Probabilities: Challenges and Outcomes of QComp

Arnd Hartmanns
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based on joint work with Carlos E. Budde, E. Moritz Hahn, Christian Hensel, Sebastian Junges, Michaela Klauck, Joachim Klein, Jan Křetínský, David Parker, Tim Quatmann, Enno Ruijters, Marcel Steinmetz, Andrea Turrini, and Zhen Zhang

QComp: A Quantitative Competition

"Friendly competition": no ranking

Semantic formalisms:

DTMC, CTMC, MDP, MA, PTA

Modelling languages:

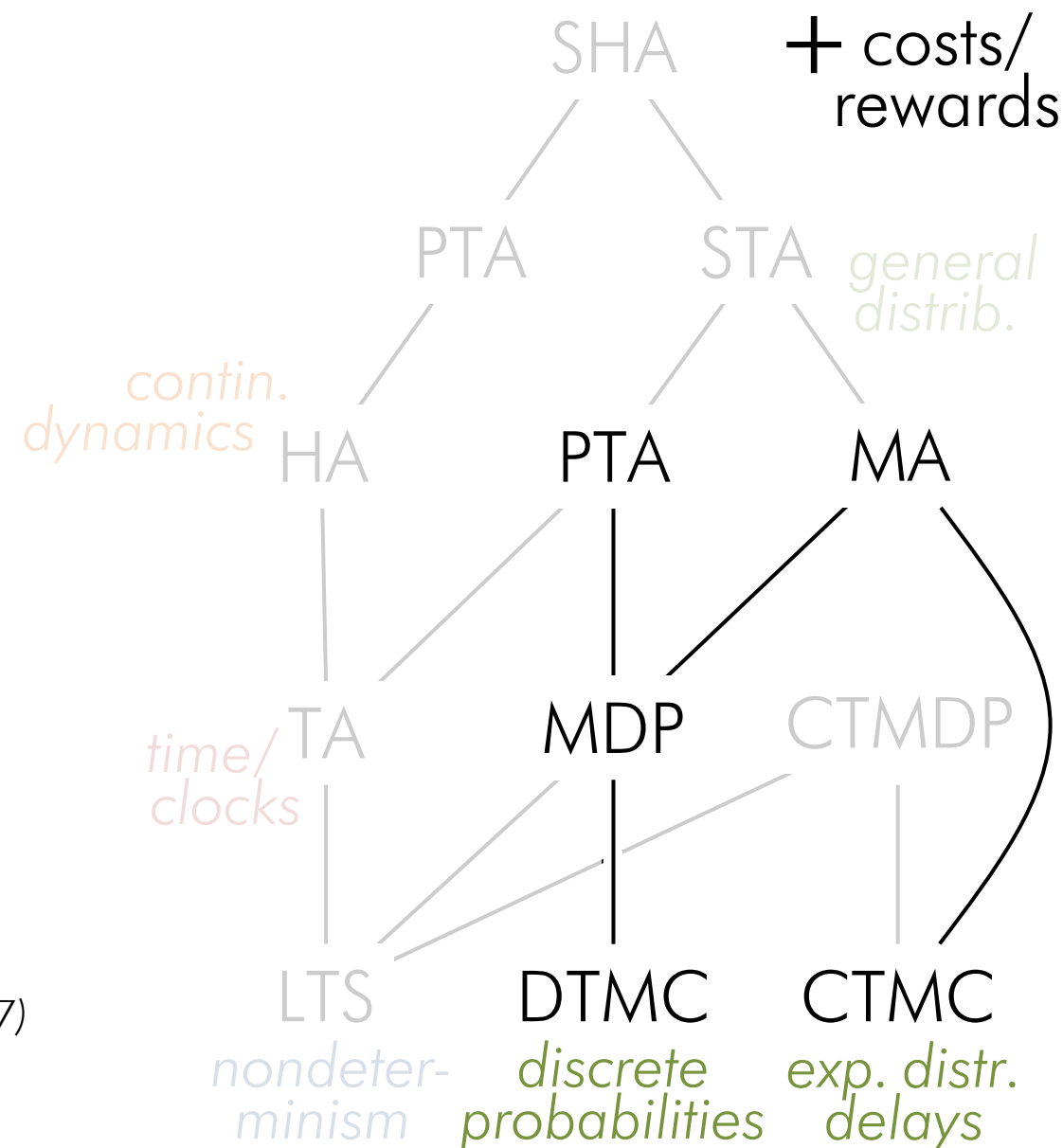
GreatSPN *stochastic Petri nets*

PPDDL *planning domains*

PRISM *general, low-level*

... *and several others*

+ JANI *model exchange format*
(jani-spec.org, TACAS'17)



QComp: A Quantitative Competition

Properties to check:

| | | |
|--------------------------|---|---------------------------------------|
| reachability probability | $\mathbb{P}(\diamond G)$ | } unbounded, time-, reward-bounded |
| expected reward | $\mathbb{E}(\text{cost} \rightarrow G)$ | |
| steady-state probability | $S(G)$ | |

Benchmarks from the Quantitative Verification Benchmark Set
all QVBS entries must have a JANI version

QVBS

TACAS 2019

qcomp.org/benchmarks

The Quantitative Verification Benchmark Set*

Arnd Hartmanns¹, Michaela Klauck², David Parker³,
 Tim Quatmann⁴, and Enno Ruijters¹

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³ University of Birmingham, Birmingham, United Kingdom

⁴ RWTH Aachen, Aachen, Germany



Search: Show all models of type (all) / GreatSPN with a Pb property and zero - infinity states

| Model | Name | Type | Original | Params | States | Properties | Notes |
|--|---------------------------|------|----------|---------|-----------------|------------------------|----------------------|
| <input checked="" type="checkbox"/> flexible-... | Flexible Manufacturing... | MA | GreatSPN | 2 (1/1) | 2.44 k - 2.70 M | 6 (2 × Pb, 2 × ...) | (small symbolic r... |
| <input checked="" type="checkbox"/> philosop... | Dining Philosophers | CTMC | GreatSPN | 2 (1/1) | 34 - 1.77 T | 3 (1 × P, 1 × Pb, ...) | (small symbolic r... |
| <input checked="" type="checkbox"/> readers-... | Readers and Writers S... | MA | GreatSPN | 1 (1/0) | 1.61 k - 101 M | 4 (2 × P, 1 × Pb, ...) | (standard GSPN ...) |

[compare results](#) (CLOSE)

The Competitors: Algorithms

Probabilistic Model Checking ^{PMC}

= numeric algorithm on full state space

— limited by state space explosion

+ ϵ -correct results: $|v - \bar{v}|/v \leq \epsilon$
(unknown) true value \uparrow computed result

Statistical Model Checking ^{SMC}

PMC:

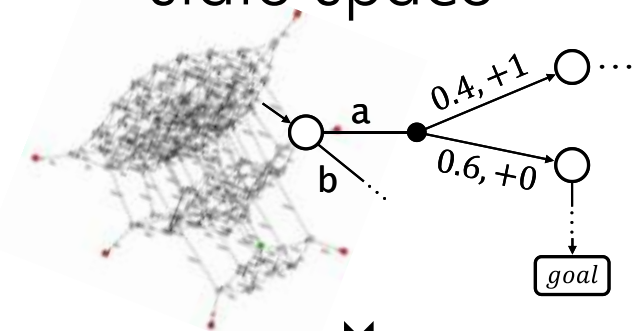
Arnd Hartmanns

formal model

```
process P() {  
  alt {  
    :: stop {= fail = true =}  
    :: send pal {  
      :95: {= done = true =}  
      : 5: reset; P()  
    } } }
```



state space



precise results

$$\mathbb{P}_{\min}(\diamond a) = 0.2035$$

$$\mathbb{P}_{\max}(\diamond a \wedge b) = 0.89$$

$$\mathbb{E}_{\min}(\#s \mid b) = 12.5$$

Probabilistic Model Checking ^{PMC}

= numeric algorithm on full state space

— limited by state space explosion

+ ϵ -correct results: $|v - \bar{v}|/v \leq \epsilon$
(unknown) true value \uparrow computed result

Statistical Model Checking ^{SMC}

= formal Monte Carlo simulation

+ constant memory usage

— rare events, nondeterminism

PAC guarantee: $\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$
 \uparrow estimate \uparrow confidence, e.g. 95%

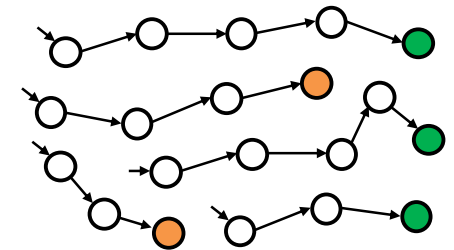
SMC:

formal model

```
process P() {  
  alt {  
    :: stop {= fail = true =}  
    :: send pal {  
      :95: {= done = true =}  
      : 5: reset; P()  
    } } }
```



sample runs



estimated results

$\mathbb{P}_{\min}(\diamond a) \approx 0.2$

$\mathbb{P}_{\max}(\diamond a \wedge b) \approx 0.9$

$\mathbb{E}_{\min}(\#s \mid b) \approx 12$

Probabilistic Model Checking ^{PMC}

= numeric algorithm on full state space

- limited by state space explosion

+ ϵ -correct results: $|v - \bar{v}| / v \leq \epsilon$

(unknown) true value computed result

Statistical Model Checking ^{SMC}

= formal Monte Carlo simulation

+ constant memory usage

- rare events, nondeterminism

PAC guarantee: $\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$

\hat{v} : estimate δ : confidence, e.g. 95 %

+ Hybrid Approaches

reinforcement learning

deep
learning

truncation

*partial exploration,
guided by simulation*

probabilistic
planning

Challenges to Correctness

Challenges to Correctness

1. Bugs in algorithms:

the algorithm itself is incorrect

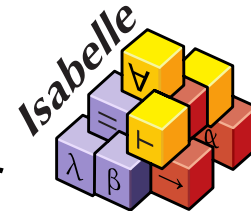
e.g. sound value iteration:
small bug in helper method
pseudocode in original paper,
wrong in 1 of 79 test models

2. Bugs in implementations:

the algorithm is correct, but the implementation is not

Acceptable?

Solutions: verify the algorithm with a theorem prover
correct-by-construction implementations
program verification



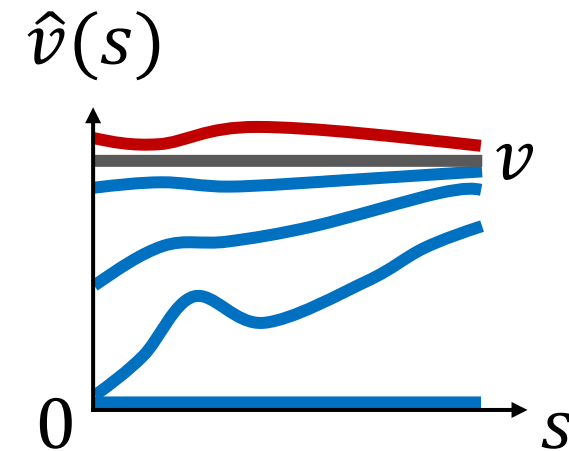
**not specific to the
quantitative setting**

Challenges to Correctness

3. Unsound algorithms:

often but not always deliver ϵ -correct result

→ value iteration and derived algorithms with one-sided approximation of the fixpoint only



Solutions: interval iteration, optimistic value iteration, BRTDP, ...

4. Floating-point implementations:

results unpredictably affected by rounding, cancellation, ...

Solutions: exact rational arithmetic, safe rounding

↑
does not scale ↑
new

**specific
to probabilistic
model checking**

Challenges to Correctness

5. The statistical error in SMC:

up 5% of the results may be totally wrong, and that's okay

Recall PAC guarantee: $\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$

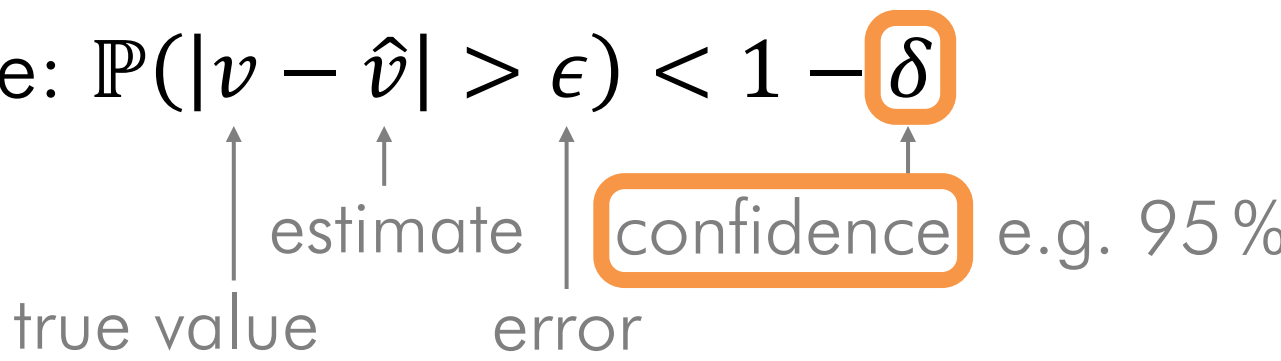


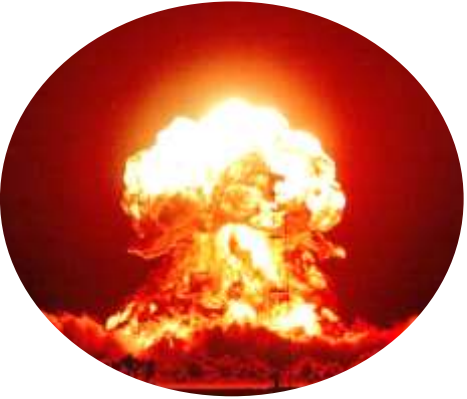
Diagram labels: true value, estimate, error, confidence, e.g. 95%

→ unavoidable in a statistical approach,
quantifiable (user-selectable confidence level)

*How can we deal with these challenges
in a tool competition?*

Correct Quantitative Competitions

Option N: *Disqualify any tool that produces just a single (ϵ -)incorrect result and publicly shame its authors*



Consequences: All SMC tools disqualified *maybe that's a good idea?*
No unsound algorithms allowed
Floating-point implementations out
→ only STORM and PRISM remain,
using their limited exact engines

Option SMC:

*Use statistical test on statistical tools
to assure confidence δ is adhered to*

**not representative of today's
quantitative verification tools**

**evaluation
time explosion**



The QComp 2020 Approach

QComp 2020: Tracks

Option QC20: *Use different tracks for different guarantees*

correct: must match true rational value where known $\epsilon = 0$

floating-point correct: must use algorithm that gives exact result, but may use floating-point arithmetic $\epsilon = 10^{-14}$

ϵ -correct: unconditionally require $|v - \bar{v}|/v \leq \epsilon$ $\epsilon = 10^{-6}$

probably ϵ -correct: require $\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$ $\epsilon = 5 \cdot 10^{-2}$
from algorithm, but we do not check this statistically

often ϵ -correct: should ensure $|v - \bar{v}|/v \leq \epsilon$, but $\epsilon = 10^{-3}$
may sometimes be wrong (also with $10'$ bound)

QComp 2020: Tools

Arnd Hartmanns

| | | | |
|---------|--------|---|-------------|
| EPMC | PMC | <i>modular tool, focus on LTL</i> | ISCAS |
| MCSTA | PMC | <i>disk-based, focus on correctness</i> | Twente |
| PRISM | PMC | <i>the original probabilistic model checker</i> | Birmingham. |
| STORM | PMC | <i>has all the algorithms and languages</i> | Aachen |
| DFTRES | SMC | <i>dynamic fault tree rare event simulator</i> | Twente |
| MODES | SMC | <i>rare events and nondeterminism</i> | Twente |
| MFPL | hybrid | <i>probabilistic planning using LRTDP</i> | Saarland |
| PET | hybrid | <i>the partial exploration tool</i> | Munich |
| STAMINA | hybrid | <i>truncation for infinite-state CTMC</i> | Utah |

| Tool | GALILEO | GREATSPN | JANI | MODEST | PGCL | PPDDL | PRISM | Properties | | | | | | | | | | | | | | | | |
|---------|---------|----------|------|--------|------|-------|-------|------------|----|---|------|----|---|---|-----|----|---|----|----|---|---|-----|----|---|
| | | | | | | | | DTMC | | | CTMC | | | | MDP | | | MA | | | | PTA | | |
| | | | | | | | | P | Pr | E | P | Pt | E | S | P | Pr | E | P | Pt | E | S | P | Pt | E |
| DFTRES | ✓ | | ✓ | | | | | + | | | + | ✓ | + | ✓ | | | | + | ✓ | + | ✓ | | | |
| ePMC | | | ✓ | | | | ✓ | ✓ | | ✓ | ✓ | ✓ | | ✓ | | ✓ | | | | | | | | |
| MCSTA | | | ✓ | ✓ | | | | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | |
| MODES | | | ✓ | ✓ | | | | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | |
| MFPL | | | ✓ | ✓ | | | | | | | | | | | + | | + | | | | | | | |
| PRISM | | | | | | | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | | | | | ✓ | ✓ | ✓ |
| PET | | | | | | | ✓ | ✓ | | | ✓ | | | | ✓ | | | | | | | | | |
| STAMINA | | | | | | | + | | | | + | | | | | | | | | | | | | |
| STORM | ✓ | ✓ | ✓ | | ✓ | | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | | | ✓ |

QComp 2020: Tools

Tool participation in the different tracks:

| track | DFTRES | ePMC | MCSTA | MODES | MFPL | PRISM | PET | STAMINA | STORM |
|---------------------------|--------|------|-------|-------|------|-------|-----|---------|-------|
| correct | — | — | — | — | — | — | — | — | ✓ |
| floating-p. | — | — | ✓ | — | — | — | — | — | ✓ |
| ε -correct | — | — | ✓ | — | — | ✓ | ✓ | — | ✓ |
| probably ε | ✓ | — | ✓ | ✓ | — | ✓ | ✓ | ✓ | ✓ |
| often ε | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| often ε (10') | ✓ | — | ✓ | ✓ | ✓ | — | ✓ | ✓ | ✓ |

→ specialised tools and generalists:
focus on specific algorithm vs. toolset

| Tool | GALILEO | GREATSPN | JANI | MODEST | PGCL | PPDDL | PRISM | Properties | | | | | | | | | | | | | | | | | | | |
|---------|---------|----------|------|--------|------|-------|-------|------------|----|---|------|----|---|-----|---|----|----|---|----|-----|---|---|----|---|---|---|---|
| | | | | | | | | DTMC | | | CTMC | | | MDP | | | MA | | | PTA | | | | | | | |
| | | | | | | | | P | Pr | E | P | Pt | E | S | P | Pr | E | P | Pt | E | S | P | Pt | E | | | |
| DFTRES | ✓ | | ✓ | | | | | + | | | + | ✓ | + | ✓ | | | | + | ✓ | + | ✓ | | | | | | |
| ePMC | | | ✓ | | | | ✓ | ✓ | | ✓ | ✓ | ✓ | | ✓ | | ✓ | | | | | | | | | | | |
| MCSTA | | | ✓ | ✓ | | | | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ |
| MODES | | | ✓ | ✓ | | | | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | + | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |
| MFPL | | | ✓ | ✓ | | | | | | | | | | + | | + | | | | | | | | | | | |
| PRISM | | | | | | | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | | | | | | | ✓ | ✓ | ✓ | ✓ | ✓ |
| PET | | | | | | | ✓ | ✓ | | | ✓ | | | | ✓ | | | | | | | | | | | | |
| STAMINA | | | | | | | + | | | | | | + | | | | | | | | | | | | | | |
| STORM | ✓ | ✓ | ✓ | | ✓ | | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ | ✓ |

QComp 2020: Tuning the Tools

Some tools provide many options and algorithms.

Which to use to win the competition?

Default configuration: evaluate tool like a non-expert user

Specific tuning per instance: showcase the tool's abilities

QComp 2020:

default = configuration *per track*, modelling formalism,
and property type recommended by authors today

specific = aggressively tuned *per instance*;
not used by all tools

**(tool defaults
may be
historical)**



A red BMW M3 is shown drifting on a track, with a large cloud of white smoke trailing behind it. The car has a yellow racing stripe across the hood with the text "STORM" and "BMW" visible. An orange and white traffic cone is in the foreground on the right. The word "STORM" is overlaid in large white letters across the front of the car.

*automatic selection of analysis configuration
based on syntactic aspects of the benchmark*

→ default/specific distinction now pointless

Pragmatic solution for QComp 2020:

STORM + STORM-STATIC

↑
automatic↑
as in QComp 2019

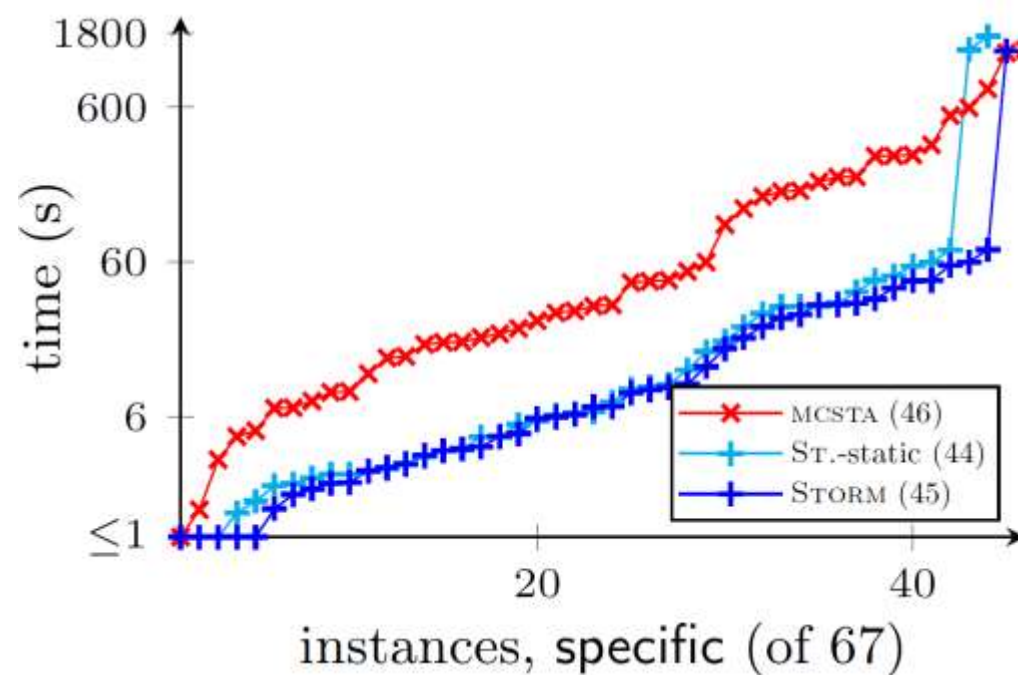
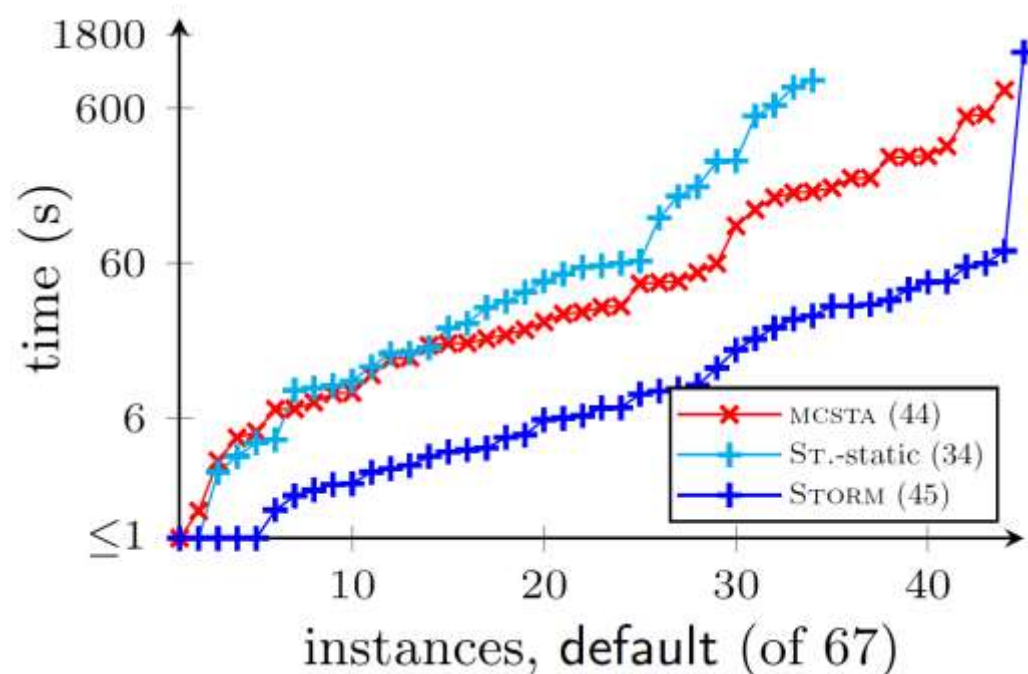
QComp 2020: The Results

QComp 2020: Results

100 benchmark instances, from the QVBS

↑
⟨model, parameters, property⟩

Quantile plots for overall comparison: **restricted to intersection**



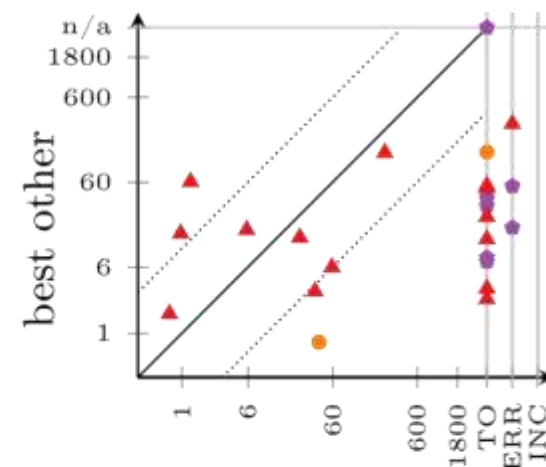
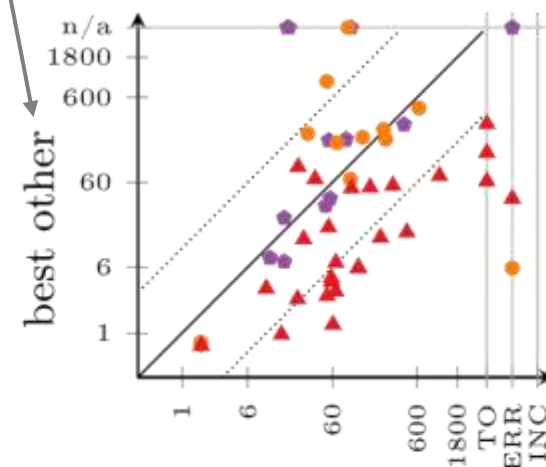
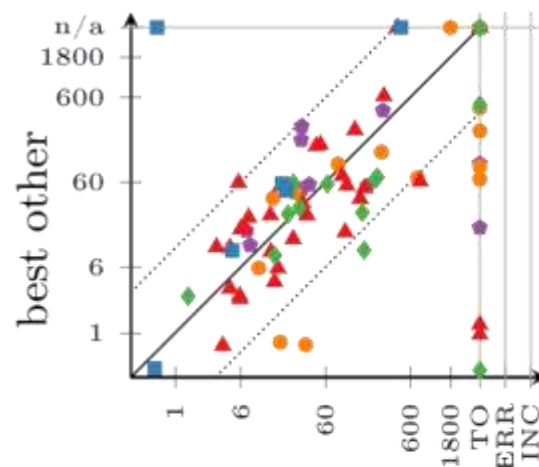
floating-point
correct track

QComp 2020: Results

ϵ -correct track:

PMC tools + PET

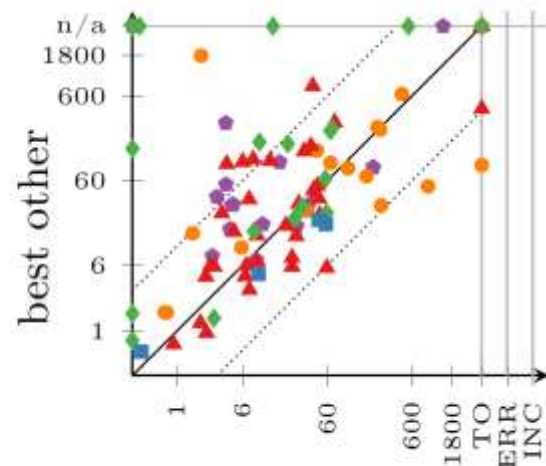
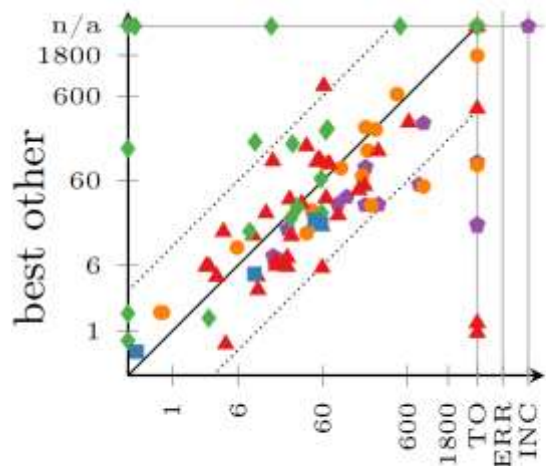
excl. STORM



MCSTA (wins 34/88)

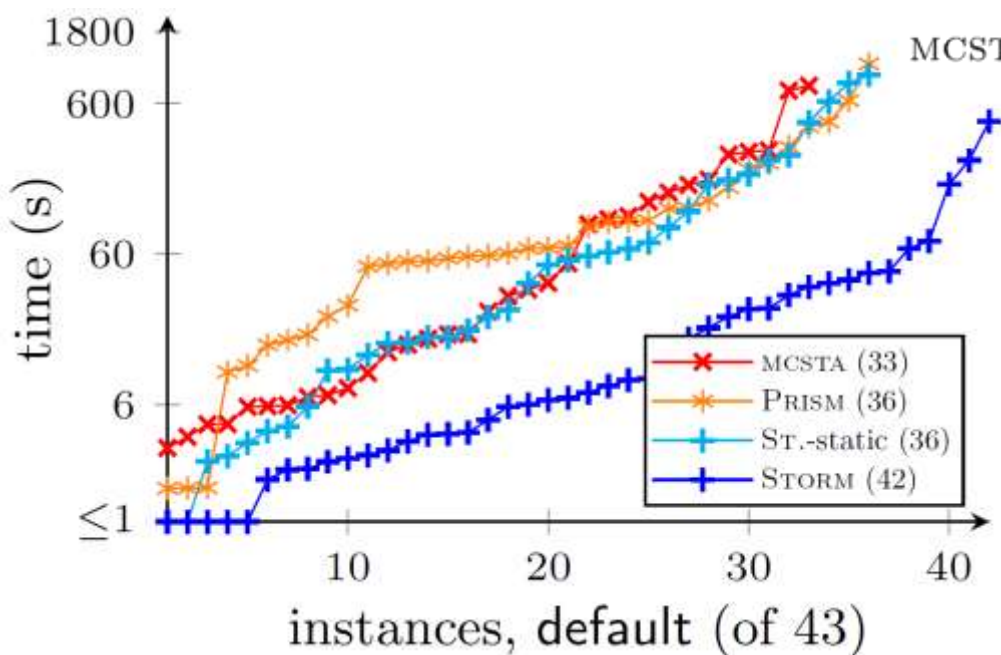
PRISM (wins 15/52)

PET (wins 4/24)



ST.-static (wins 34/96)

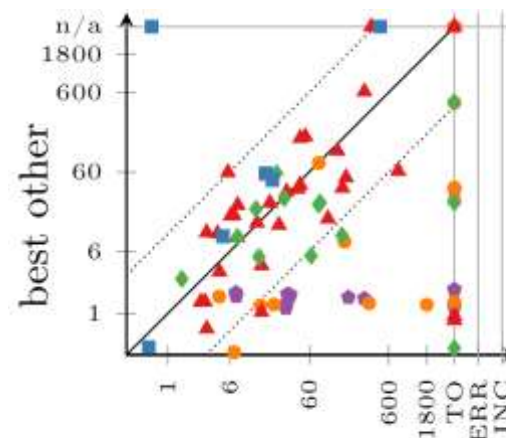
STORM (wins 54*/96)



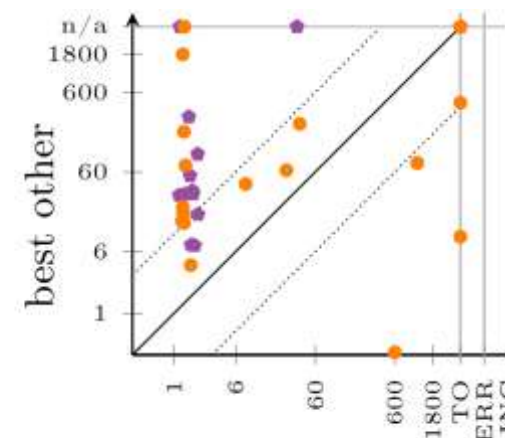
→ scatter plots show more details

QComp 2020: Results

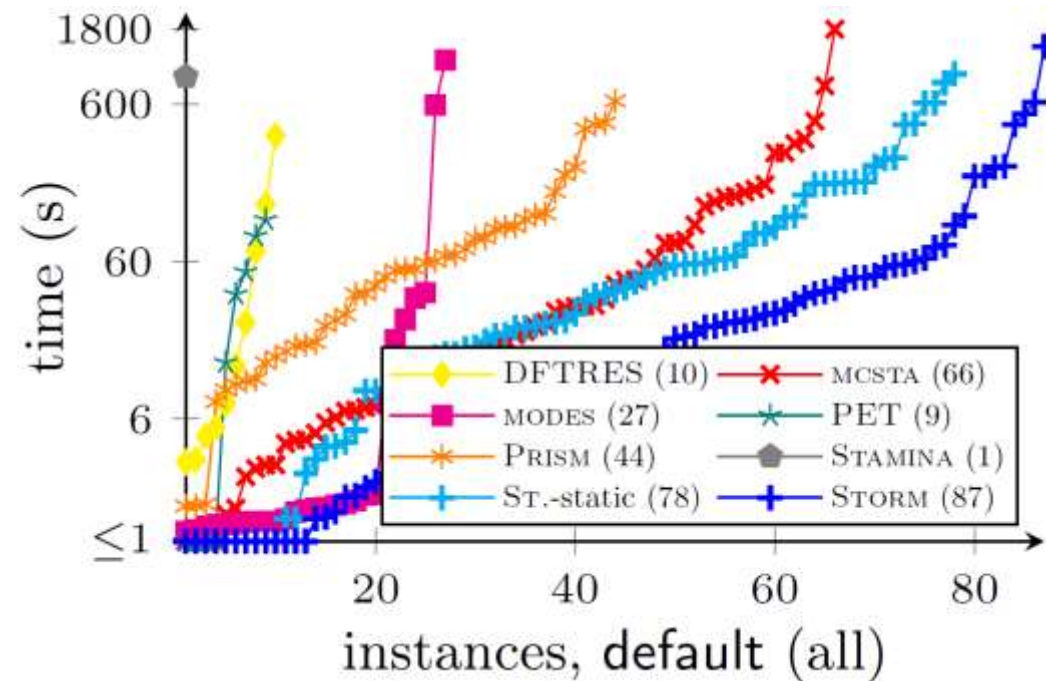
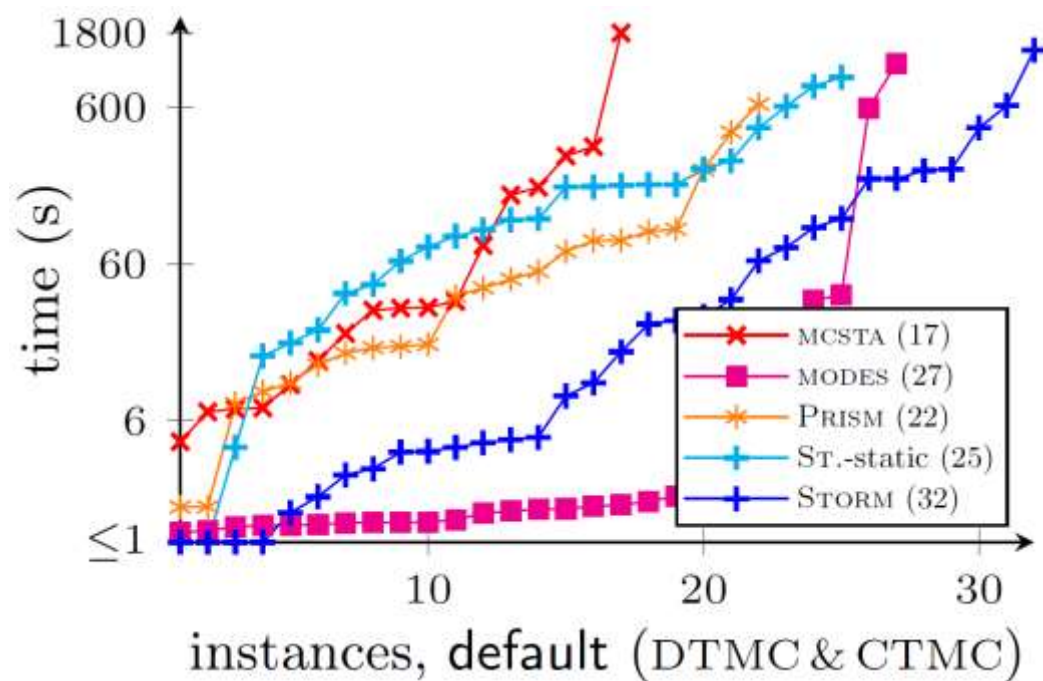
Probably ϵ -correct track:
showcase for statistical
model checkers



MCSTA (wins 24/88)



MODES (wins 24/32)



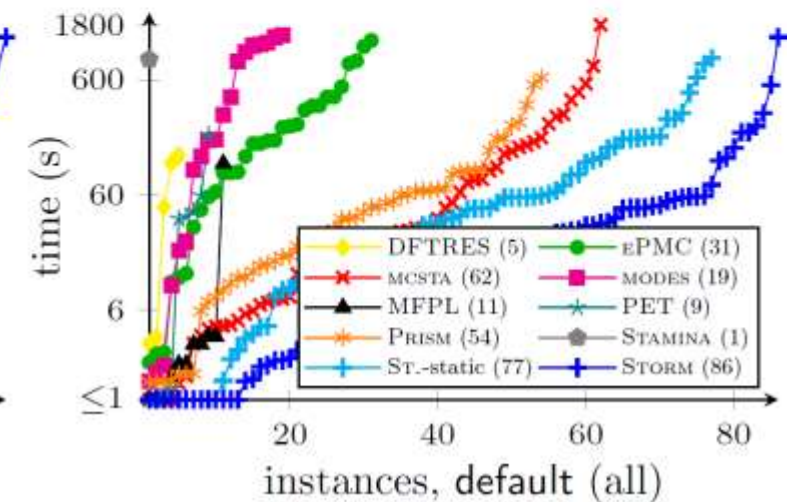
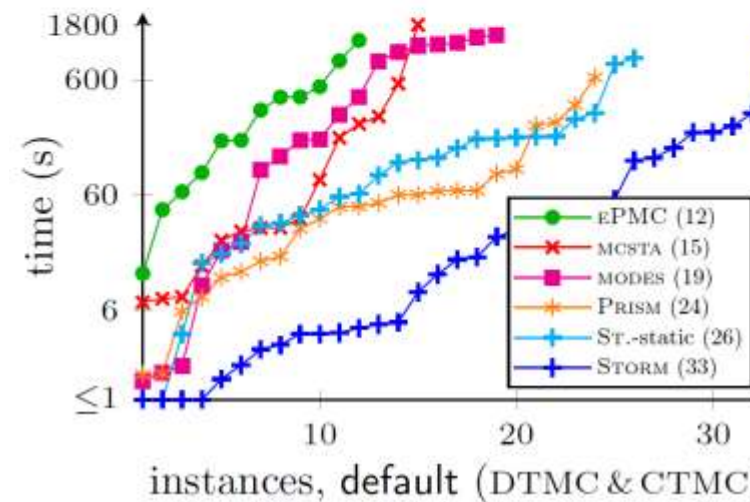
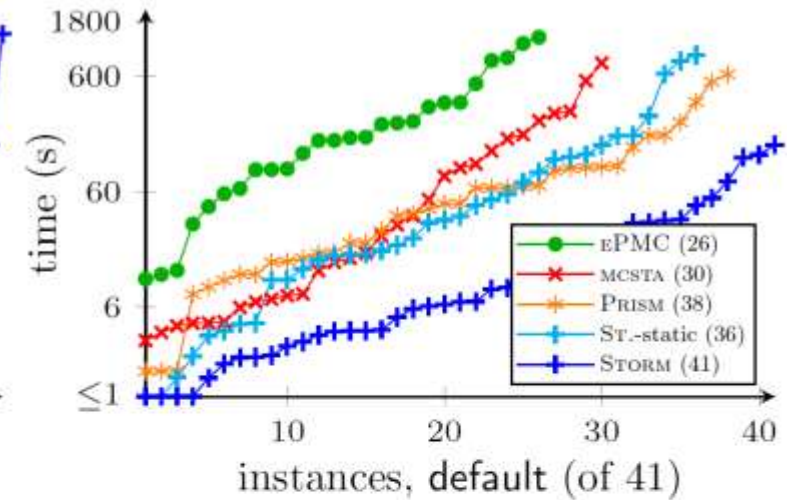
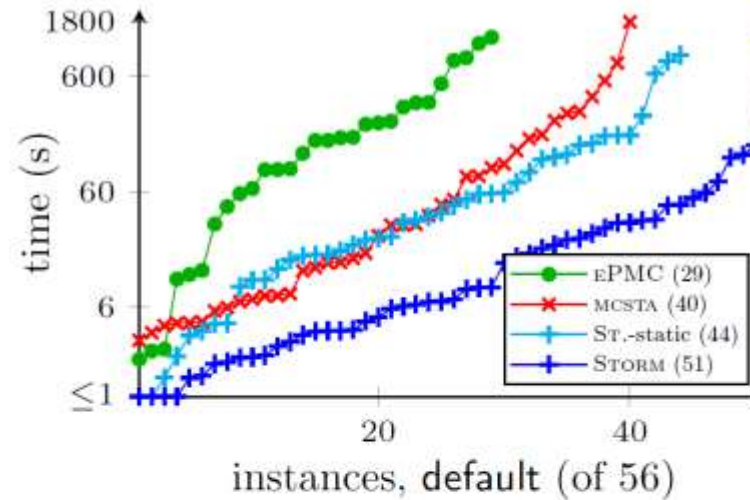
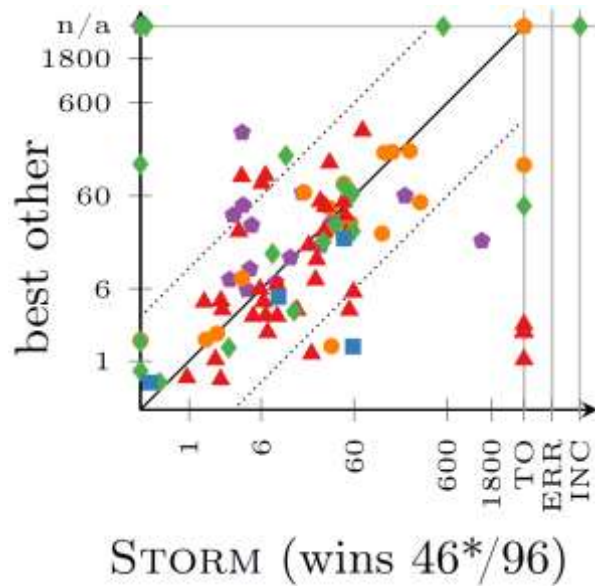
→ quantile plots show whatever you want

QComp 2020: Results

Often ϵ -correct track:

- compare with 2019
- 10' version useless

Who is the winner?



Summary

Quantitative verification: **PMC**, **SMC**, and hybrid approaches

Challenges: *algorithm bugs*

unsound algorithms

implementation bugs

statistical error

**specific to
quantitative
setting**

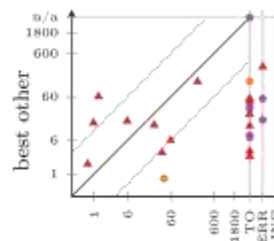
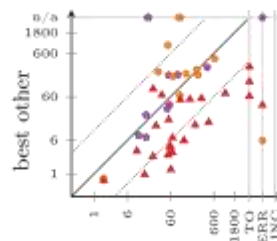
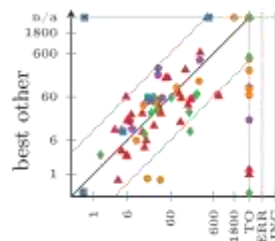
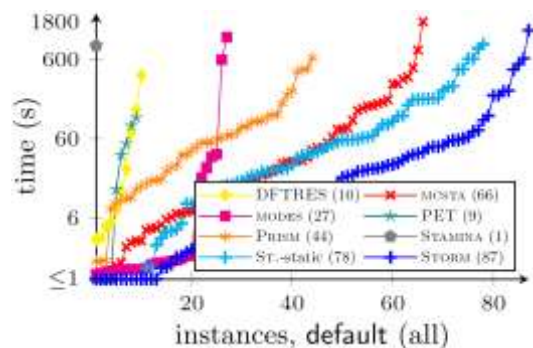
no exact results

$$|v - \bar{v}|/v \leq \epsilon$$

floating-point errors

$$\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$$

QComp 2020: 5 tracks 100 benchmarks
9 tools default + specific



qcomp.org

On Correctness, Precision, and
Performance in Quantitative Verification*
QComp 2020 Competition Report

Carlos E. Budde¹, Arnd Hartmanns¹, Michaela Klauk²,
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Competing with Probabilities

+ a tuned STORM

FormaliSE 2022

*10th Int. Conference on Formal
Methods in Software Engineering*

Co-located with ICSE 2022
May 22-23, Pittsburgh, USA

Deadlines (tentative):

Jan 20: paper submission
Jan 27: artifacts (voluntary)

Papers: 10 pages, ACM format

...more info at

formalise.org

Advertisement

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RRRR 2022

*1st Workshop on Reproducibility
& Replication of Research Results*

Co-located with ETAPS 2022
April 2, Munich, Germany

Deadlines (tentative):

Feb 1: short papers (6 pages)
Feb 15: extended abstracts

Informal proceedings,
extended papers in STTT

*...see **qcomp.org/rrrr/2022***

Summary

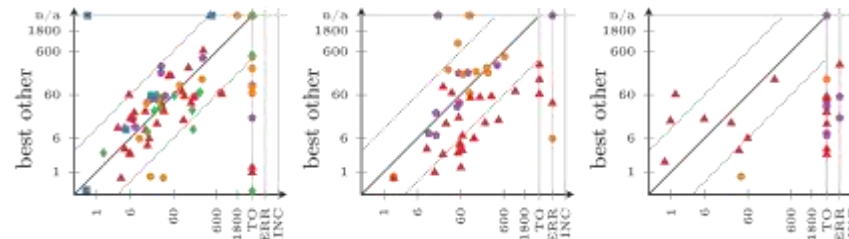
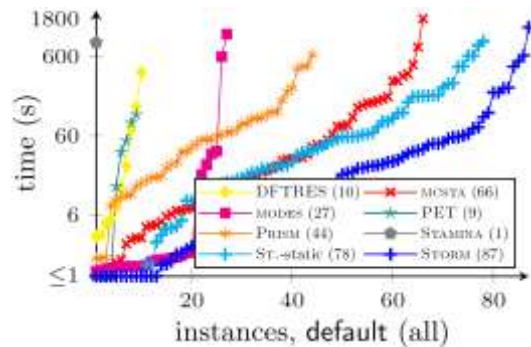
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Challenges: *algorithm bugs* *unsound algorithms*
implementation bugs *statistical error*

**specific to
quantitative
setting**

no exact results $|v - \bar{v}|/v \leq \epsilon$ floating-point errors
 $\mathbb{P}(|v - \hat{v}| > \epsilon) < 1 - \delta$

QComp 2020: 5 tracks 100 benchmarks
 9 tools default + specific



+ a tuned STORM

qcomp.org

On Correctness, Precision, and
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