

Understanding mobility in networks: A node embedding approach

Matheus F. C. Barros¹, **Carlos H. G. Ferreira**^{1,2,4}, Bruno Pereira dos Santos¹,
Lourenço A. P. Júnior³, Marco Mellia⁴ and Jussara M. Almeida²

¹ Universidade Federal de Ouro Preto - Brazil

² Universidade Federal de Minas Gerais - Brazil

³ Aeronautics Institute of Technology - Brazil

⁴ Politecnico di Torino - Italy

Mobility in network

Understanding the entities mobility patterns plays a fundamental role in the design, management, and performance of applications and services

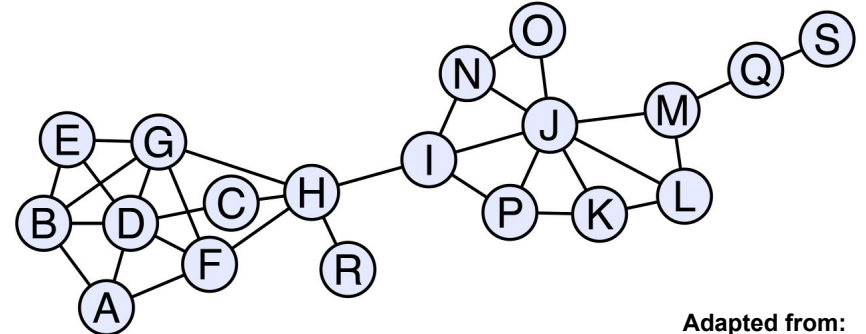


Source: <https://www.urban-hub.com/pt-br/smart-mobility/>

Mobility in network



Source: <https://www.urban-hub.com/pt-br/smart-mobility/>

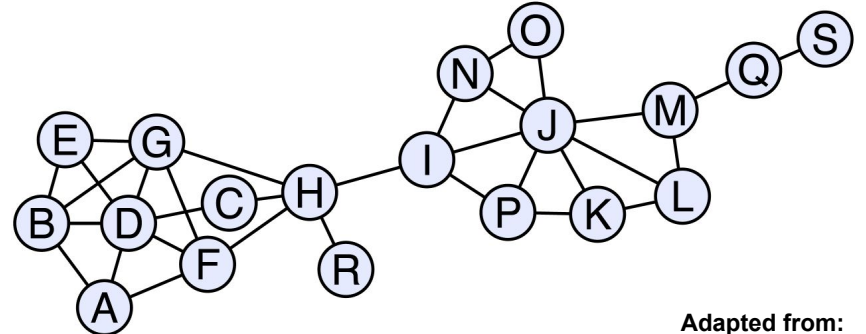


Adapted from:
https://ocw.mit.edu/courses/civil-and-environmental-engineering/1-022-introduction-to-network-models-fall-2018/lecture-notes/MIT1_022F18_lec4.pdf

Mobility in network



Source: <https://www.urban-hub.com/pt-br/smart-mobility/>

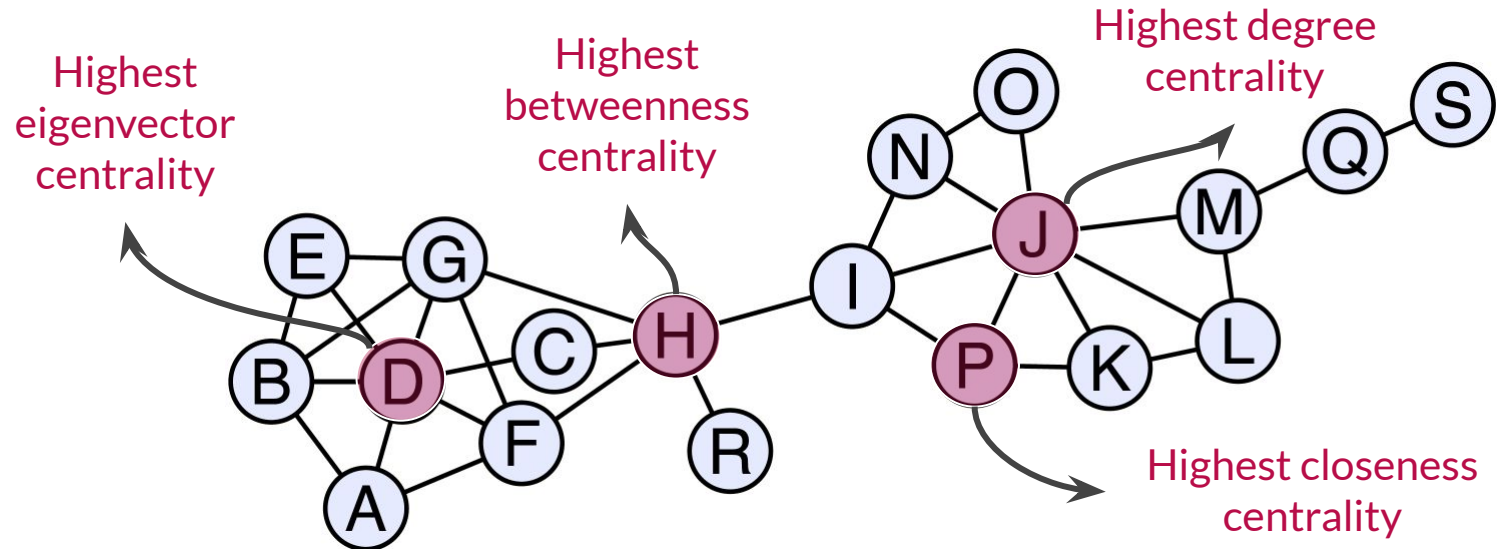


Adapted from:
https://ocw.mit.edu/courses/civil-and-environmental-engineering/1-022-introduction-to-network-models-fall-2018/lecture-notes/MIT1_022F18_lec4.pdf

Many solutions were proposed based on topological measures

Motivation

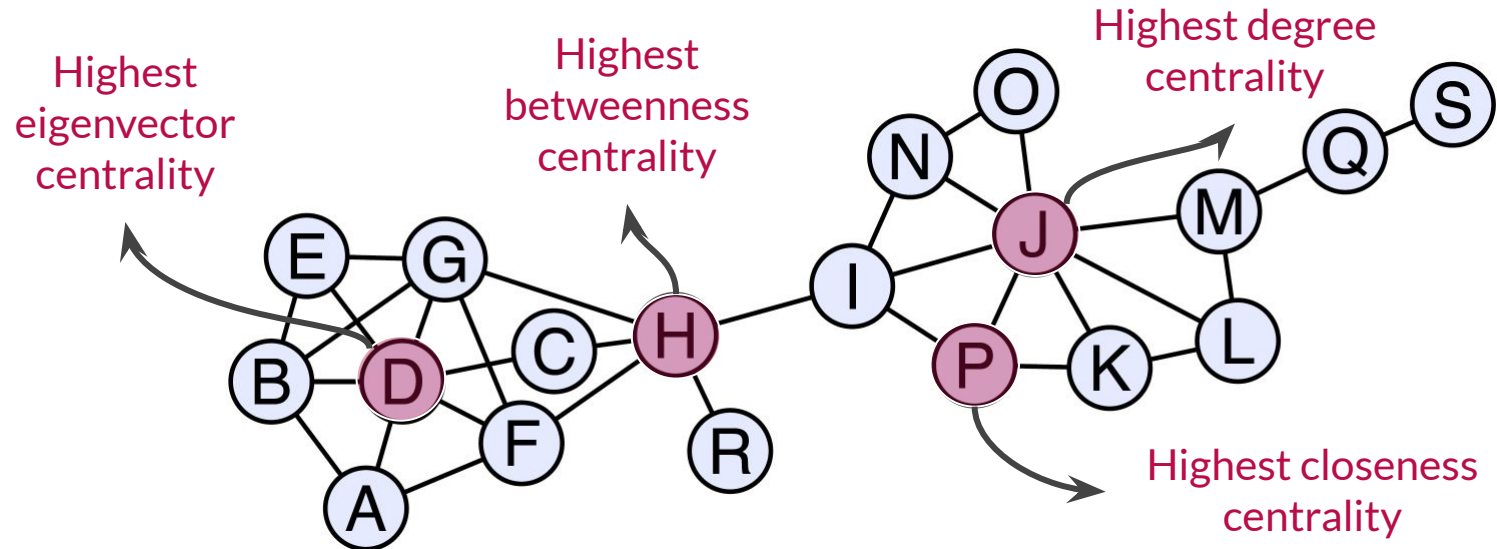
Each measure provides a **distinct notion of importance** for a **node**!



Adapted from: https://ocw.mit.edu/courses/civil-and-environmental-engineering/1-022-introduction-to-network-models-fall-2018/lecture-notes/MIT1_022F18_lec4.pdf

Motivation

Each measure provides a **distinct notion of importance** for a **node**!



Adapted from: https://ocw.mit.edu/courses/civil-and-environmental-engineering/1-022-introduction-to-network-models-fall-2018/lecture-notes/MIT1_022F18_lec4.pdf

They cannot **generalize** the **nodes' importance criteria**!

Our Goal

Propose a node embedding-based methodology to model and analyze the mobility pattern over spatial and temporal dimensions

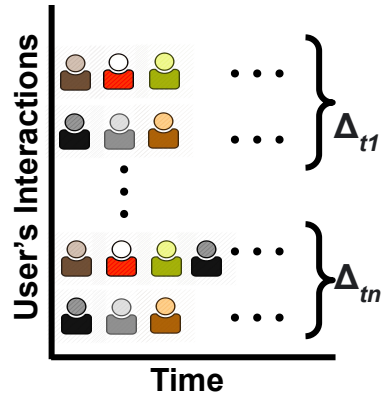
Our Goal

Propose a node embedding-based methodology to model and analyze the mobility pattern over spatial and temporal dimensions

Focus is to capture the **nodes' mobility** and **importance** for connectivity using the network topology and its temporal evolution

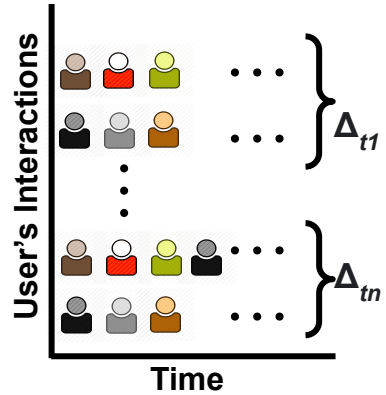
Methodology

Dataset

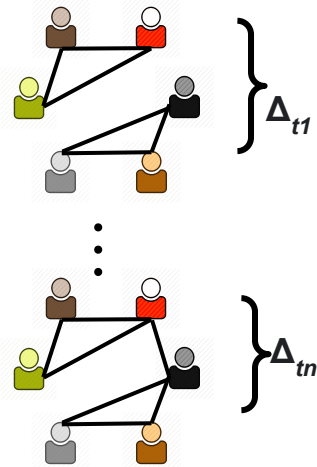


Methodology

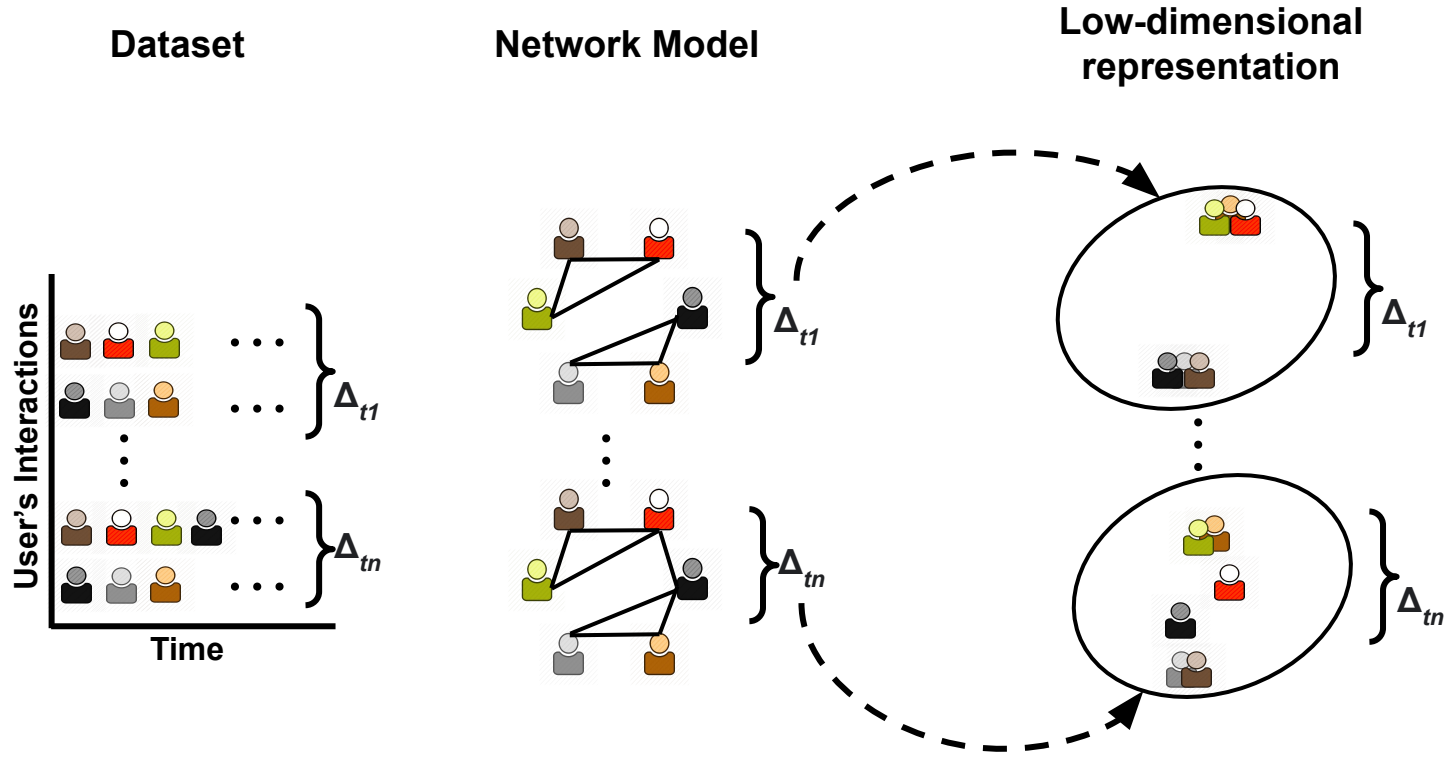
Dataset



Network Model

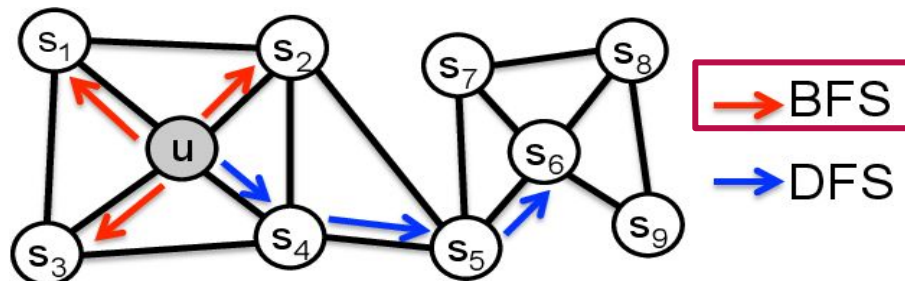


Methodology



DynamicNode2Vec

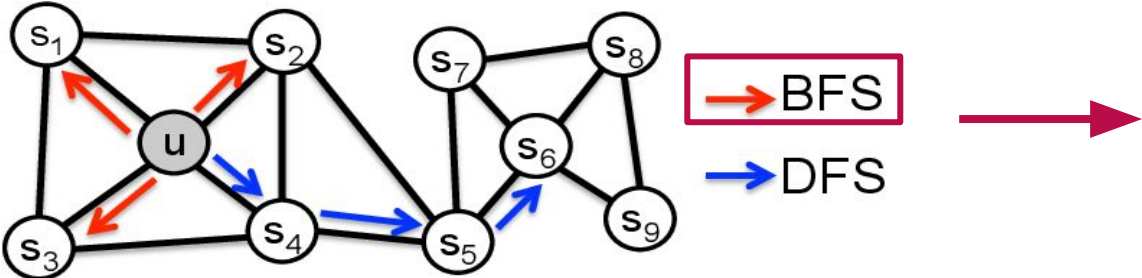
For each G_{Δ_t} , it performs a sampling using a biased random walker:



Source: Node2vec: Scalable Feature Learning for Networks. A. Grover, J. Leskovec.
ACM SIGKDD International Conference on Knowledge Discovery and Data Mining (KDD), 2016.

DynamicNode2Vec

For each G_{Δ_t} , it performs a sampling using a biased random walker:

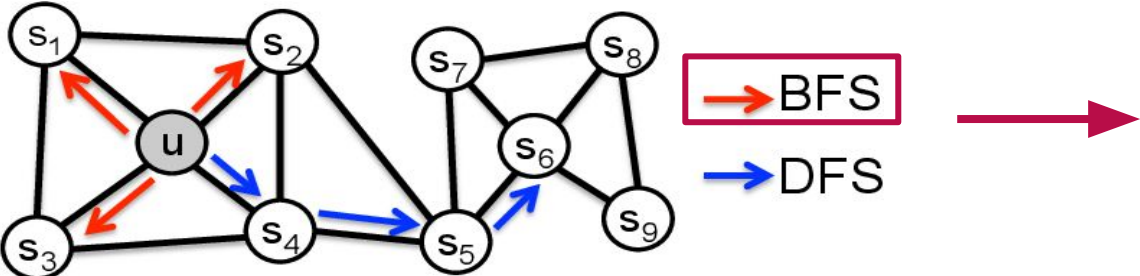


	S1	S2	S3	S4	S5	S6	S7	S8	S9
S1	0	15	14	7	7	2	0	2	2
S2		0	12	18	6	1	1	2	1
S3			0	18	17	15	4	5	6
S4				0	13	8	3	2	7
S5					0	13	10	11	19
S6						0	15	17	20
S7							0	16	17
S8								0	15
S9									0

Source: Node2vec: Scalable Feature Learning for Networks. A. Grover, J. Leskovec. ACM SIGKDD International Conference on Knowledge Discovery and Data Mining (KDD), 2016.

DynamicNode2Vec

For each G_{Δ_t} , it performs a sampling using a biased random walker:



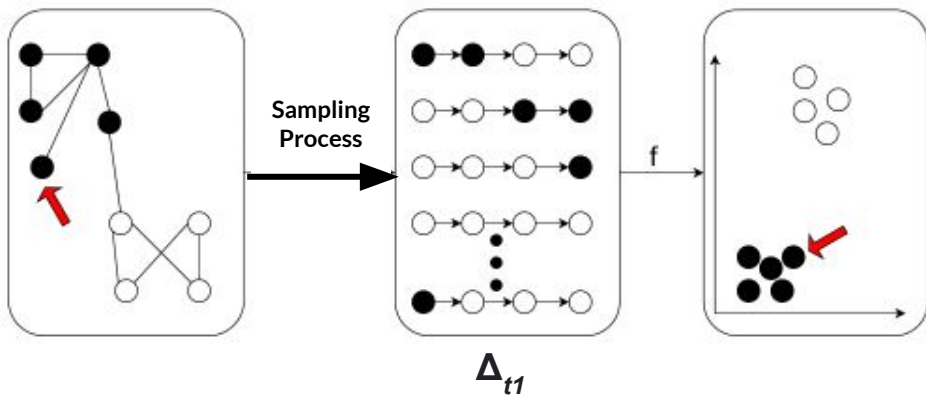
Source: Node2vec: Scalable Feature Learning for Networks. A. Grover, J. Leskovec. ACM SIGKDD International Conference on Knowledge Discovery and Data Mining (KDD), 2016.

	S1	S2	S3	S4	S5	S6	S7	S8	S9
S1	0	15	14	7	7	2	0	2	2
S2		0	12	18	6	1	1	2	1
S3			0	18	17	15	4	5	6
S4				0	13	8	3	2	7
S5					0	13	10	11	19
S6						0	15	17	20
S7							0	16	17
S8								0	15
S9									0

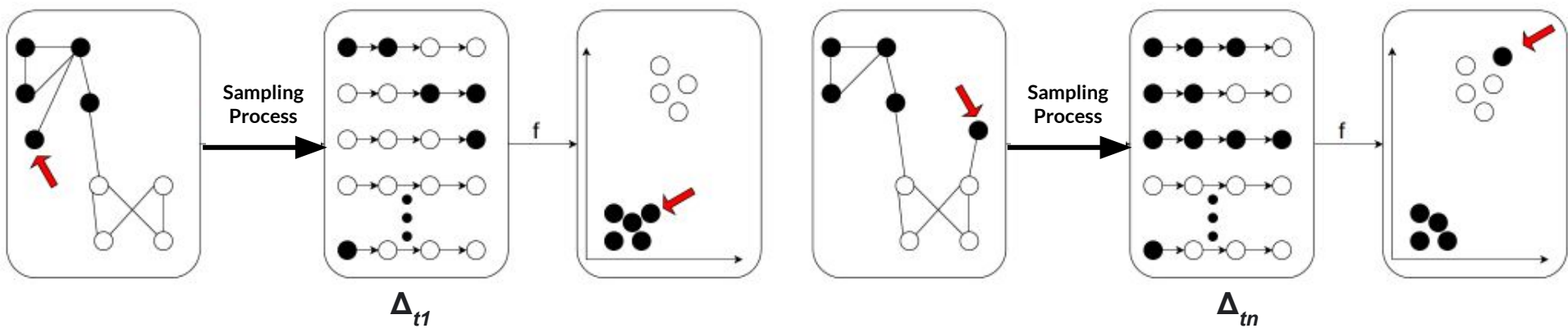
Intuition: The greater the co-occurrence between two nodes, the closer they are in the network, and the more important is the connection between them

Use the co-occurrences to produce a sequence of **time-aligned embeddings**

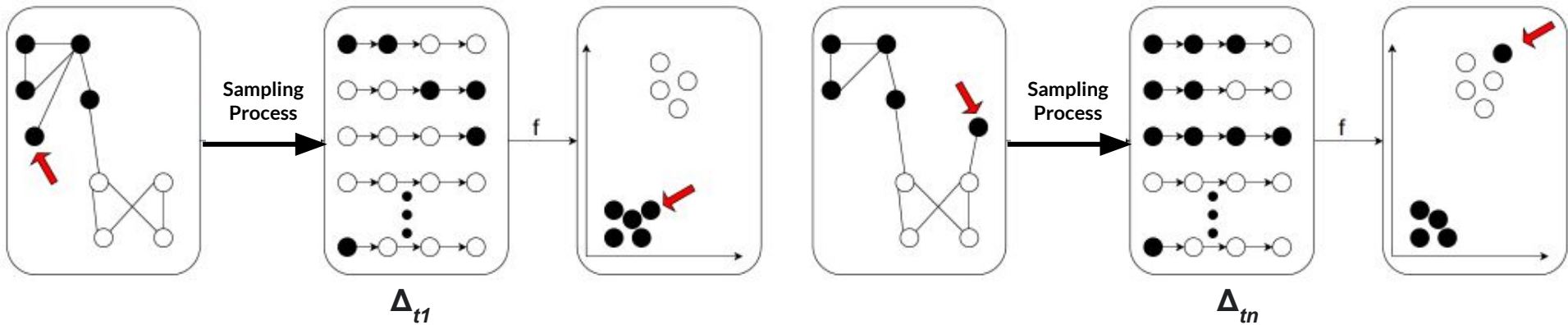
DynamicNode2Vec: The temporal embeddings



DynamicNode2Vec: The temporal embeddings

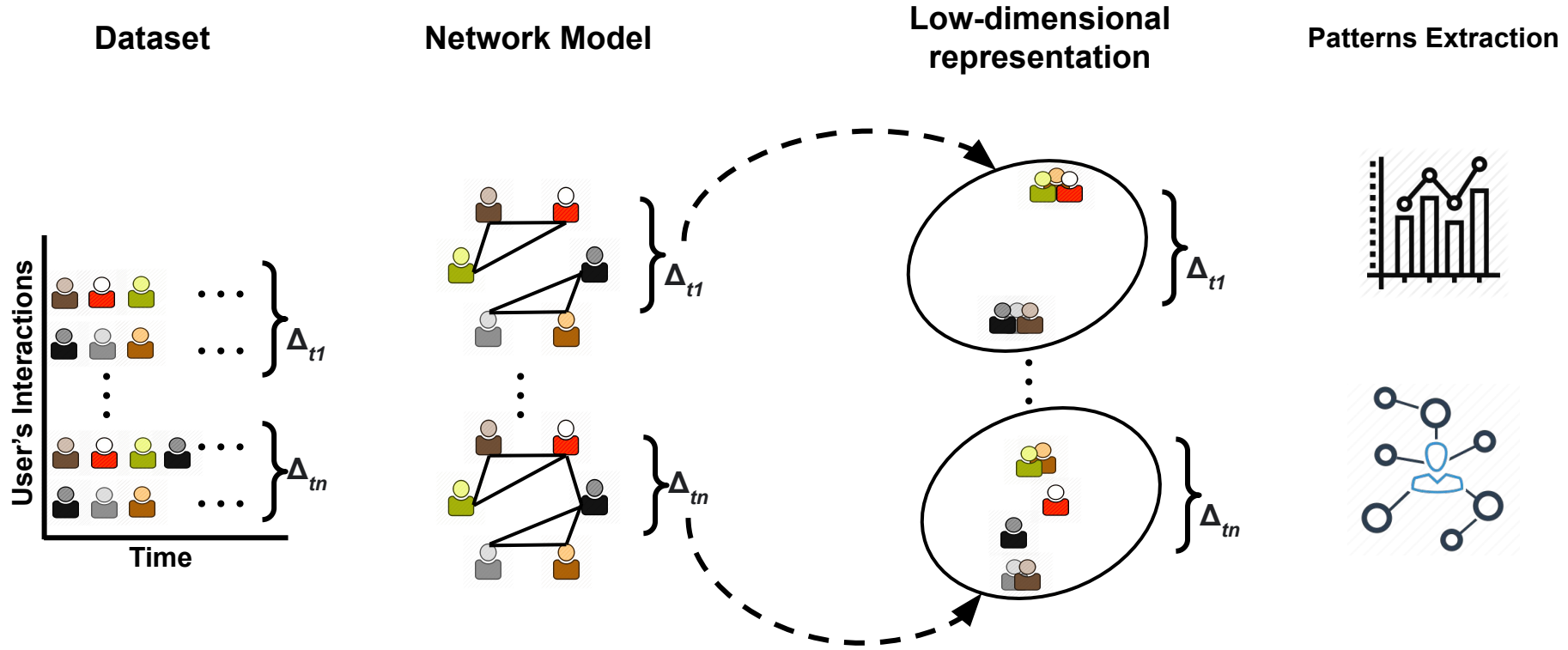


DynamicNode2Vec: The temporal embeddings



Allow **tracking** to what extent nodes **change their connections** over time!

Methodology



Extracting temporal mobility patterns

Cosine distance: Quantifies the node **connection changes** between two distinct time windows

- Values close to 0 indicate that the node keeps its connections to the same nodes in the two compared time windows while 1 is the opposite

Vector norm: By design, the more a node appears in the sampled paths in a given time window, the greater is the norm of its vector

- Indicates the node's **importance to network connectivity**

Case Study

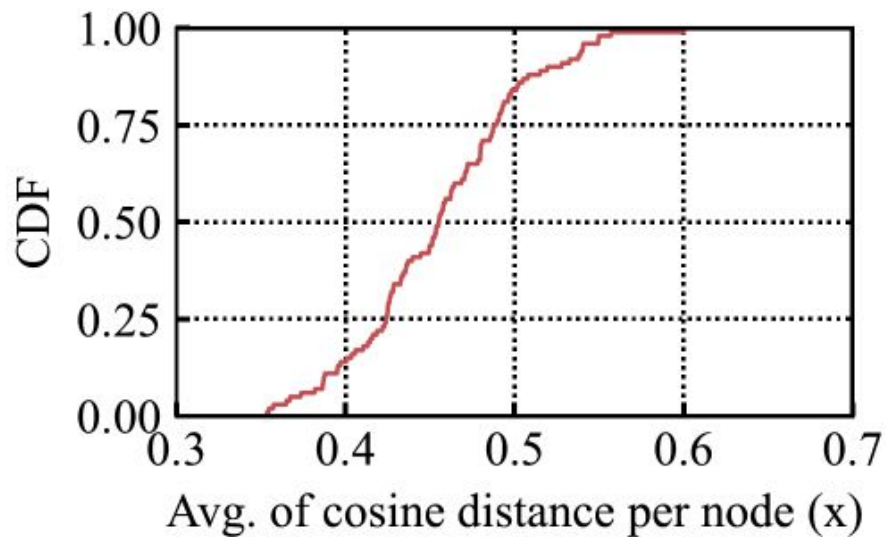
Group Regularity Mobility Model:

- Based on the **dynamics** and **regularity** of social meetings
 - Considers **cyclical** and **sporadic** meetings
- Generate synthetic traces with real properties

Our dataset:

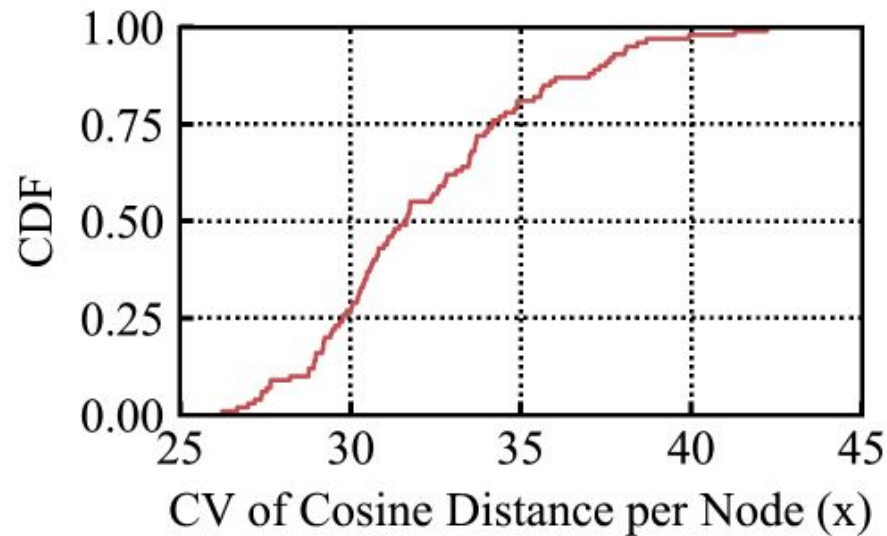
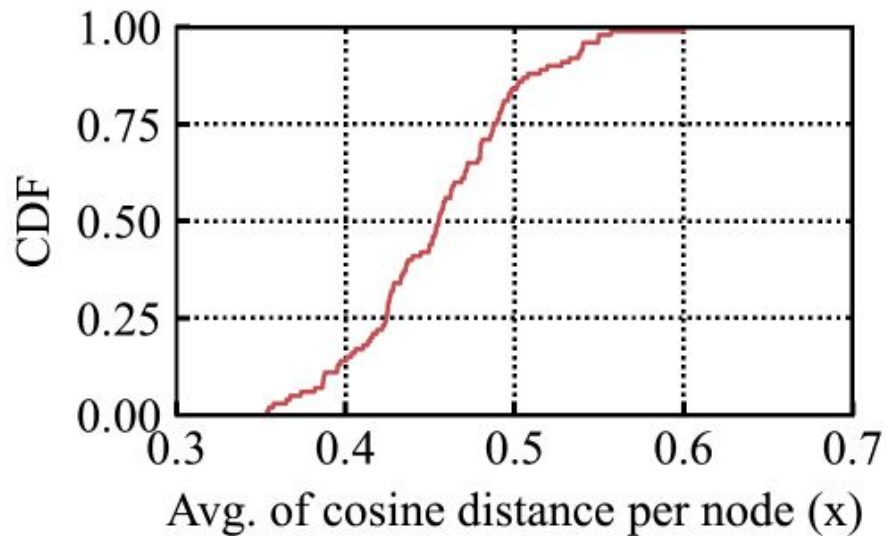
- 100 users
- Covering a period of 87 days
- Daily time windows

To what extent do nodes change their connections?



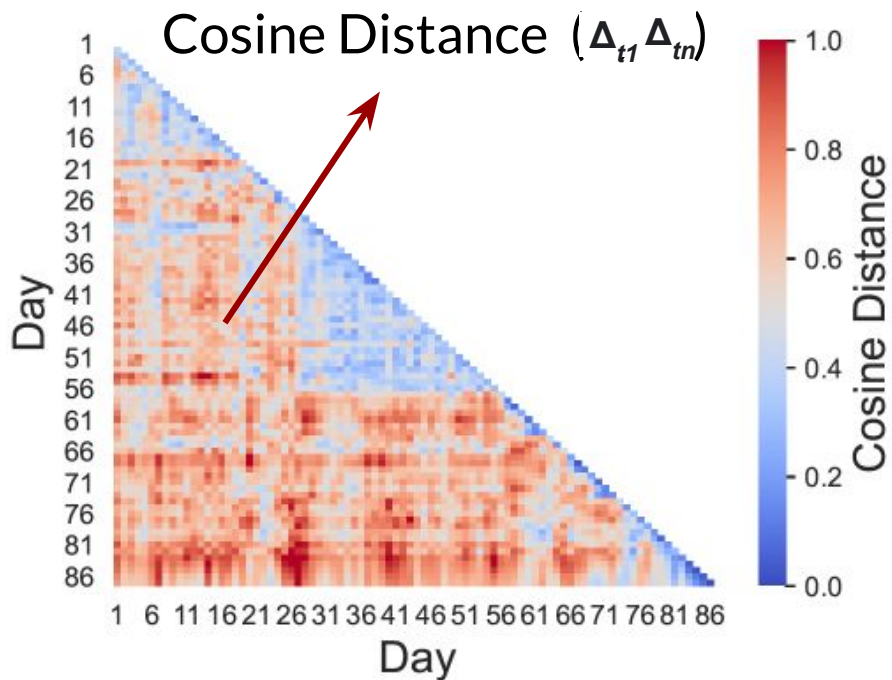
Nodes with **different levels** of **mobility**

To what extent do nodes change their connections?



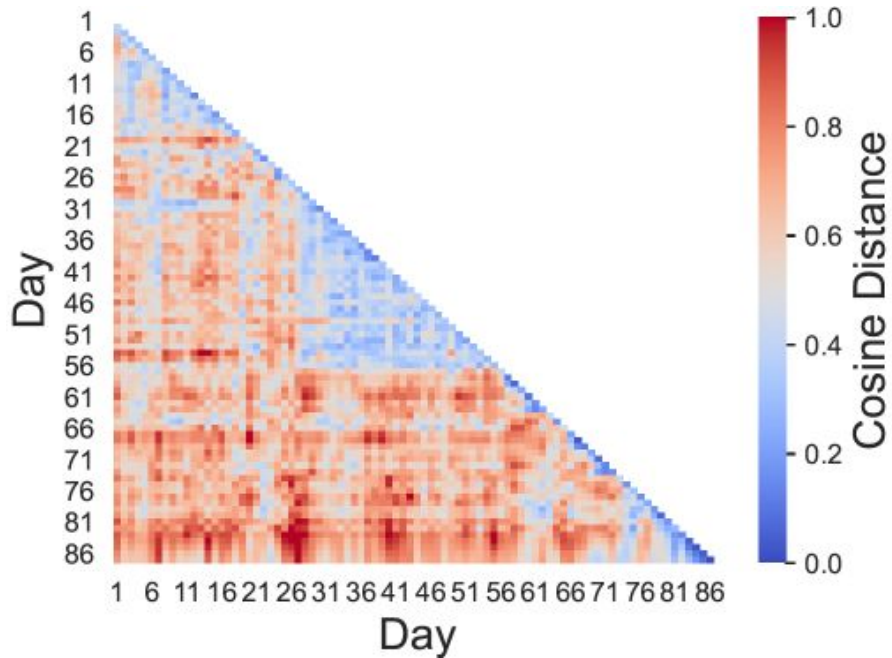
High **CV** indicates that these **changes** tend to be **irregular**

To what extent do nodes change their connections?

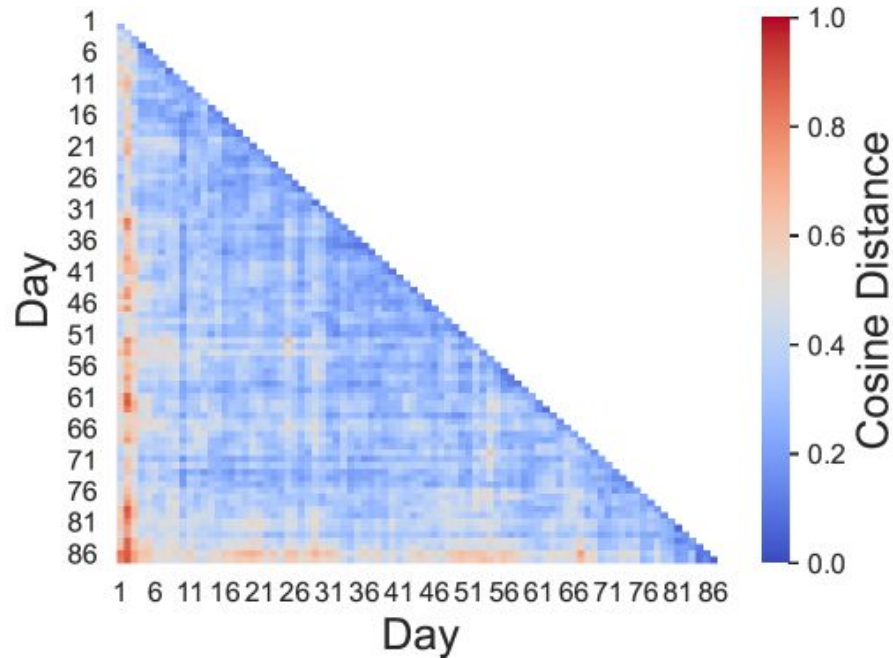


Node pattern with the
highest avg. cosine distance

To what extent do nodes change their connections?

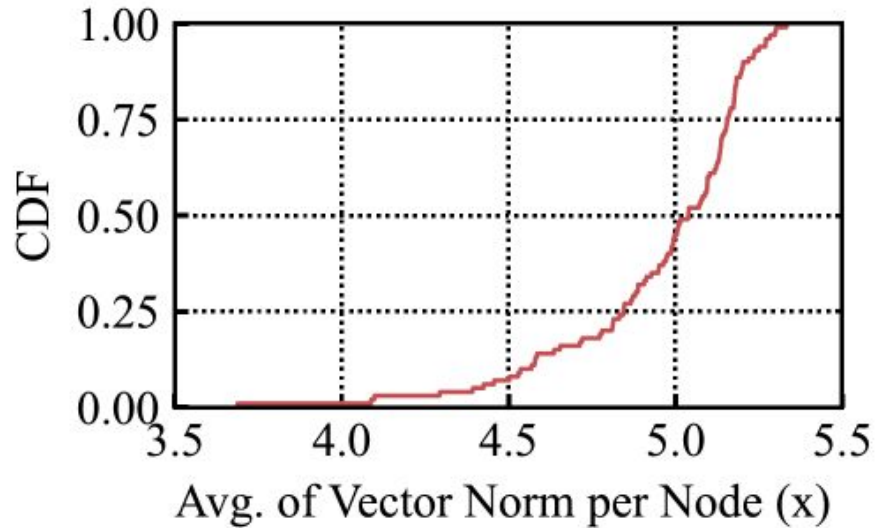


Node pattern with the **highest** avg. cosine distance



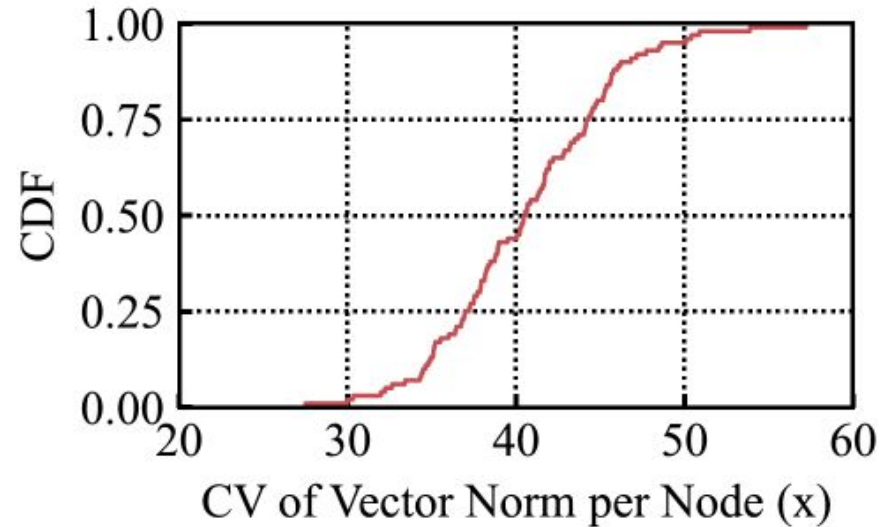
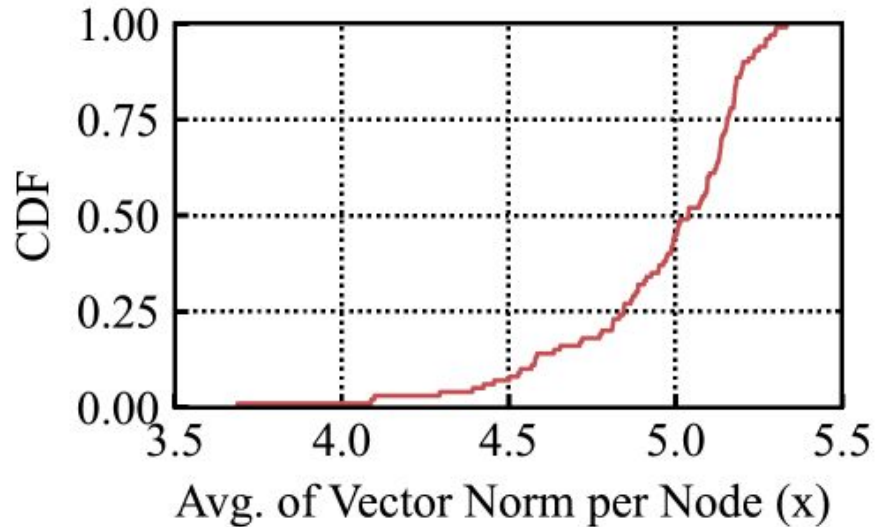
Node pattern with the **lowest** avg. cosine distance

How important are the connections established by them?



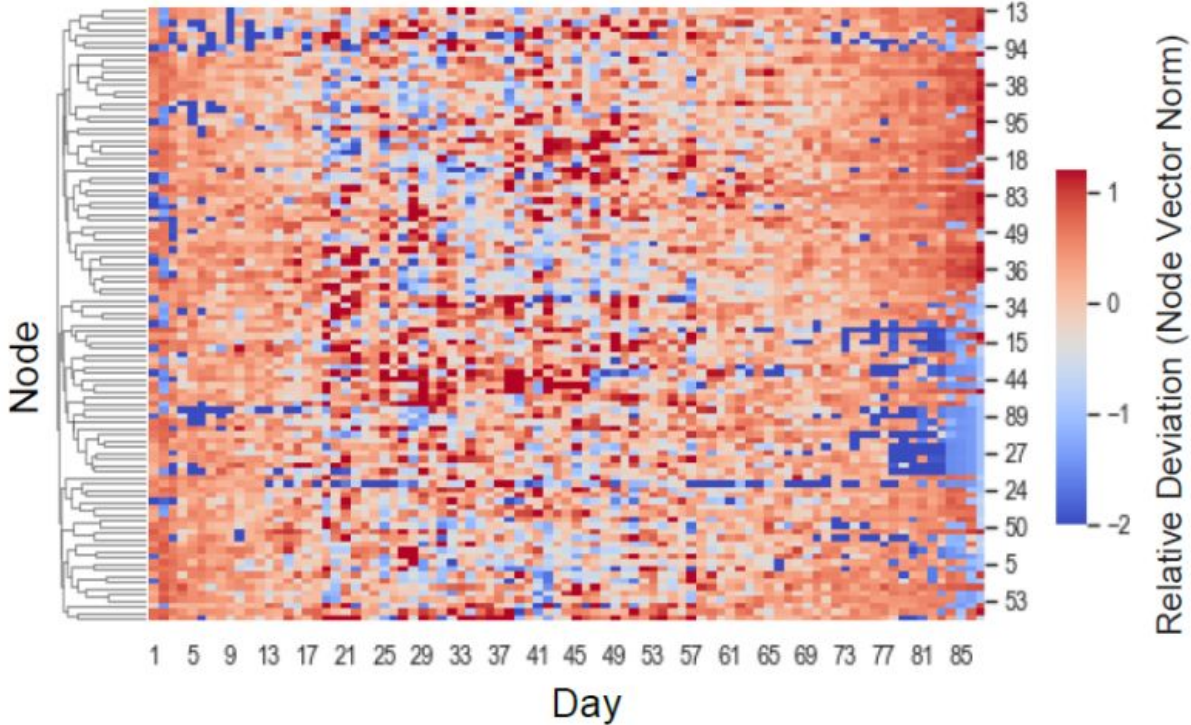
Nodes with **different levels of importance**

How important are the connections established by them?

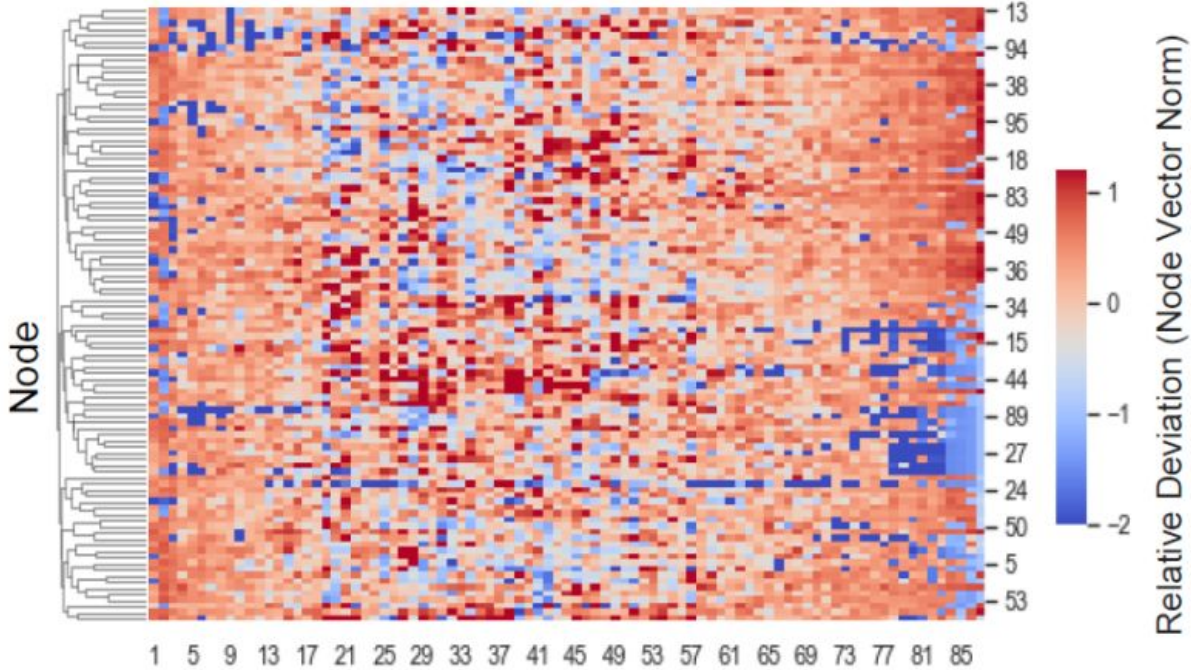


High **variation** around the average suggests that **nodes** have **temporary importance**

How important are the connections established by them?

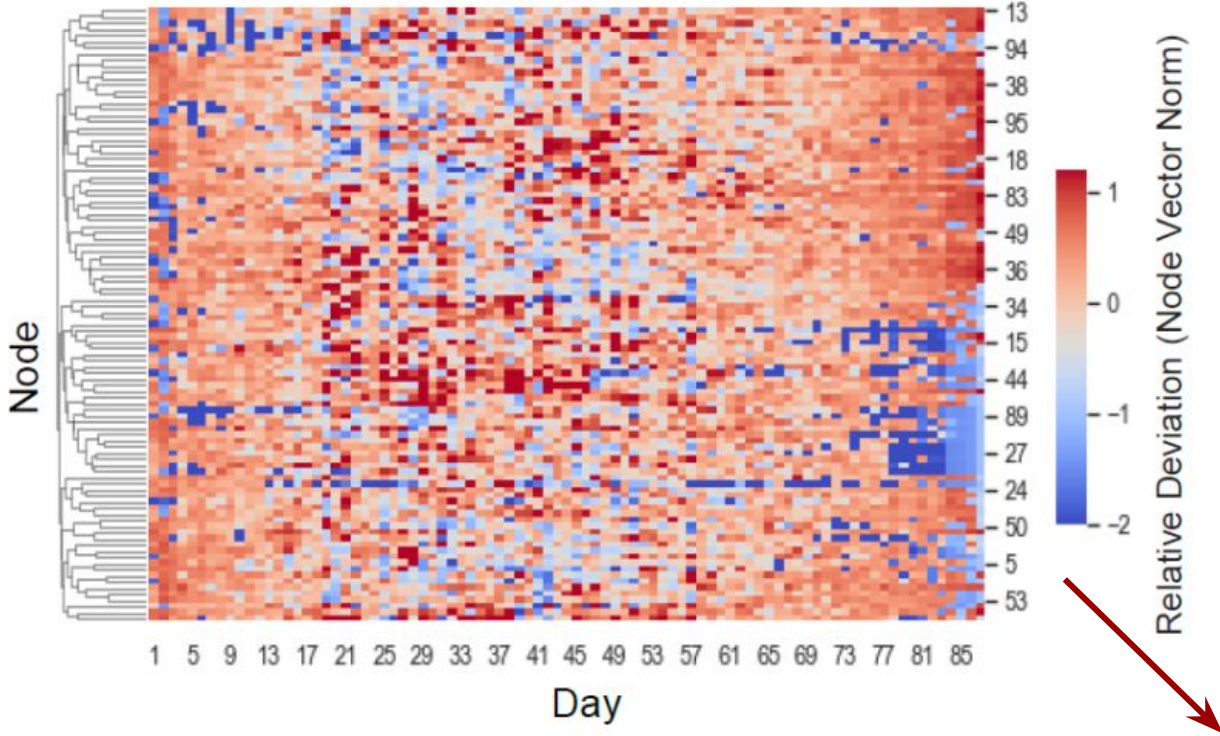


How important are the connections established by them?



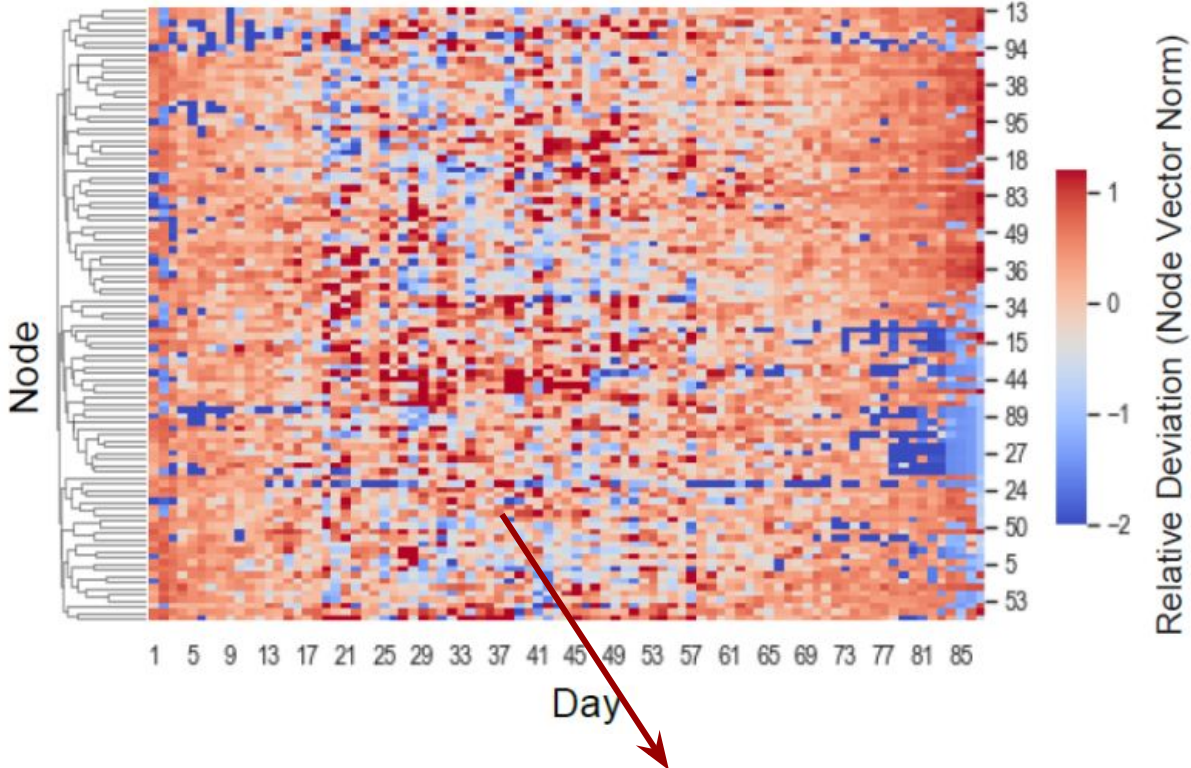
Day  Period observed

How important are the connections established by them?



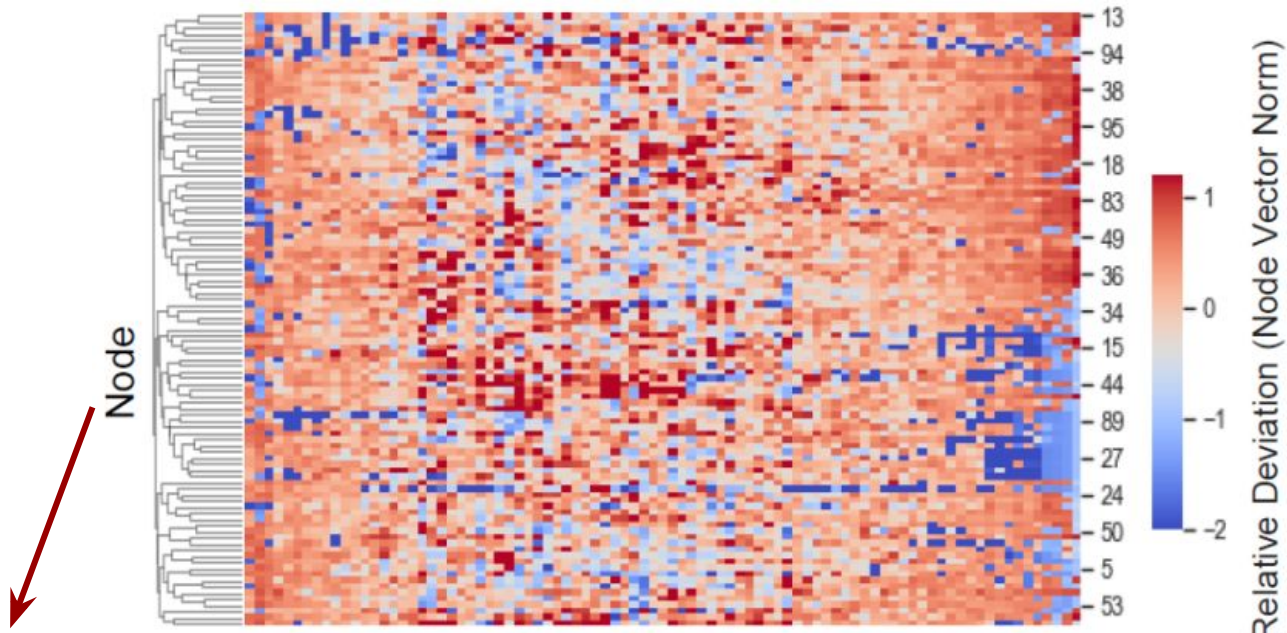
Nodes (people)

How important are the connections established by them?



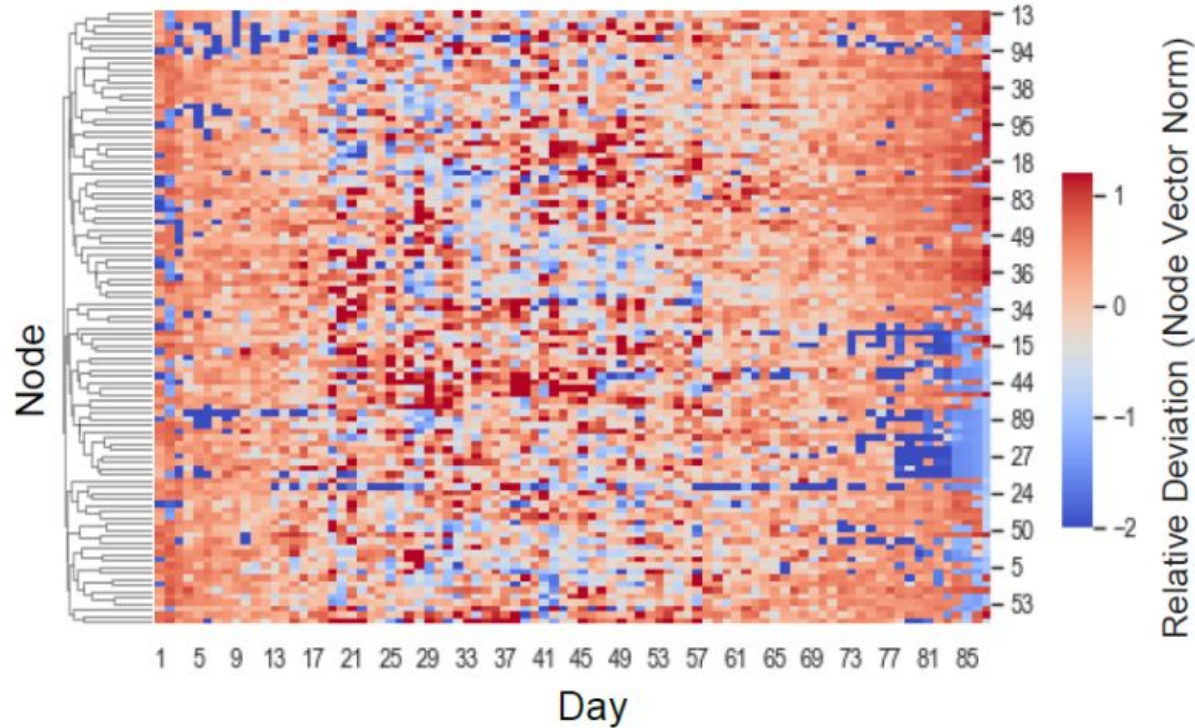
Vector norm of a node representation (normalized z-score)

How important are the connections established by them?



Dendrogram indicating nodes of similar importance in the same days

How important are the connections established by them?



Groups of nodes have momentary connectivity importance

What about topological measurements?

Embedding	Topological	Correlation
Avg. of Cosine Distance	Avg. of Degree	-0.64
Avg. of Cosine Distance	Avg. of Betweenness	-0.69
Avg. of Cosine Distance	Avg. of Closeness	-0.64
Avg. of Cosine Distance	Avg. of Eigenvector	-0.65
Avg. of Cosine Distance	Avg. of Clustering Coefficient	0.51
Avg. of Vector Norm	Avg. of Degree	0.33
Avg. of Vector Norm	Avg. of Betweenness	0.50
Avg. of Vector Norm	Avg. of Closeness	0.28
Avg. of Vector Norm	Avg. of Eigenvector	0.32
Avg. of Vector Norm	Avg. of Clustering Coefficient	-0.55

What about topological measurements?

Embedding	Topological	Correlation
Avg. of Cosine Distance	Avg. of Degree	-0.64
Avg. of Cosine Distance	Avg. of Betweenness	-0.69
Avg. of Cosine Distance	Avg. of Closeness	-0.64
Avg. of Cosine Distance	Avg. of Eigenvector	-0.65
Avg. of Cosine Distance	Avg. of Clustering Coefficient	0.51
Avg. of Vector Norm	Avg. of Degree	0.33
Avg. of Vector Norm	Avg. of Betweenness	0.50
Avg. of Vector Norm	Avg. of Closeness	0.28
Avg. of Vector Norm	Avg. of Eigenvector	0.32
Avg. of Vector Norm	Avg. of Clustering Coefficient	-0.55

They suggest that the **more dynamic** a node is, the **lower its** centrality

What about topological measurements?

Embedding	Topological	Correlation
Avg. of Cosine Distance	Avg. of Degree	-0.64
Avg. of Cosine Distance	Avg. of Betweenness	-0.69
Avg. of Cosine Distance	Avg. of Closeness	-0.64
Avg. of Cosine Distance	Avg. of Eigenvector	-0.65
Avg. of Cosine Distance	Avg. of Clustering Coefficient	0.51
Avg. of Vector Norm	Avg. of Degree	0.33
Avg. of Vector Norm	Avg. of Betweenness	0.50
Avg. of Vector Norm	Avg. of Closeness	0.28
Avg. of Vector Norm	Avg. of Eigenvector	0.32
Avg. of Vector Norm	Avg. of Clustering Coefficient	-0.55

Centrality measurements are not capable of generalizing the connectivity importance

Conclusions and Future Work

Our approach offers an **alternative notion** of **connectivity importance**

Allow for **tracking connectivity importance** while the connections in the network evolve **over time**

Suggest that topological network measures **could not generalize the patterns of connectivity** captured here

Conclusions and Future Work

Our approach offers an **alternative notion** of **connectivity importance**

Allow for **tracking connectivity importance** while the connections in the network evolve **over time**

Suggest that topological network measures **could not generalize the patterns of connectivity** captured here

As future work:

- Incorporate it into solutions for dissemination/collection of information in mobile networks
 - Evaluate the performance of such protocols comparing purely topological measures to those proposed here

Thanks!

E-mail: chgferreira@ufop.edu.br