

The Effect of Network Topology on Credit Network Throughput

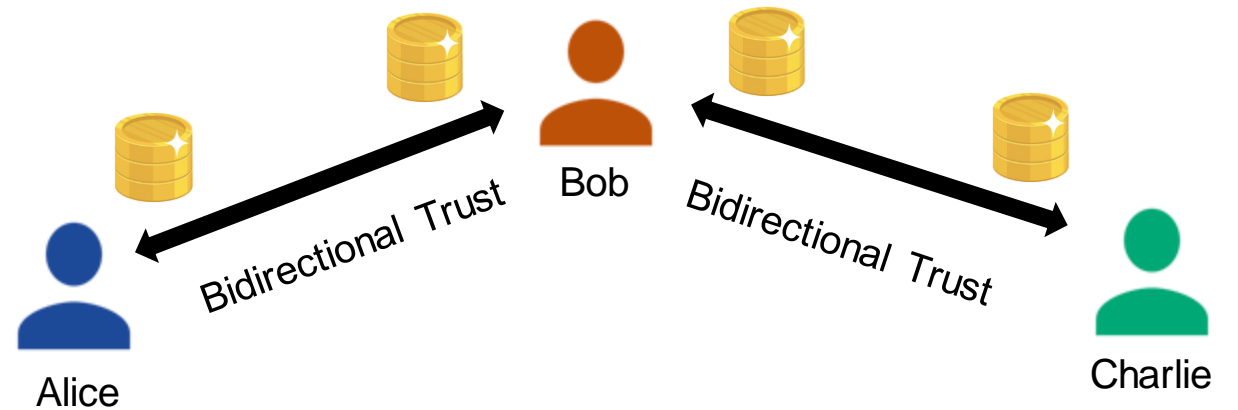
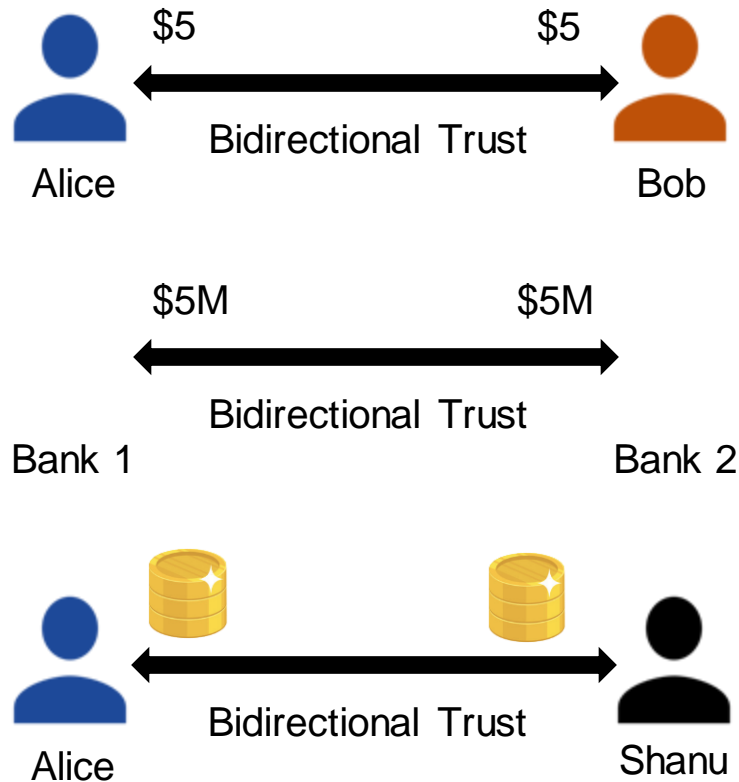
Vibhaalakshmi Sivaraman, Weizhao Tang,
Shaileshh Bojja Venkatakrisnan, Giulia Fanti, Mohammad





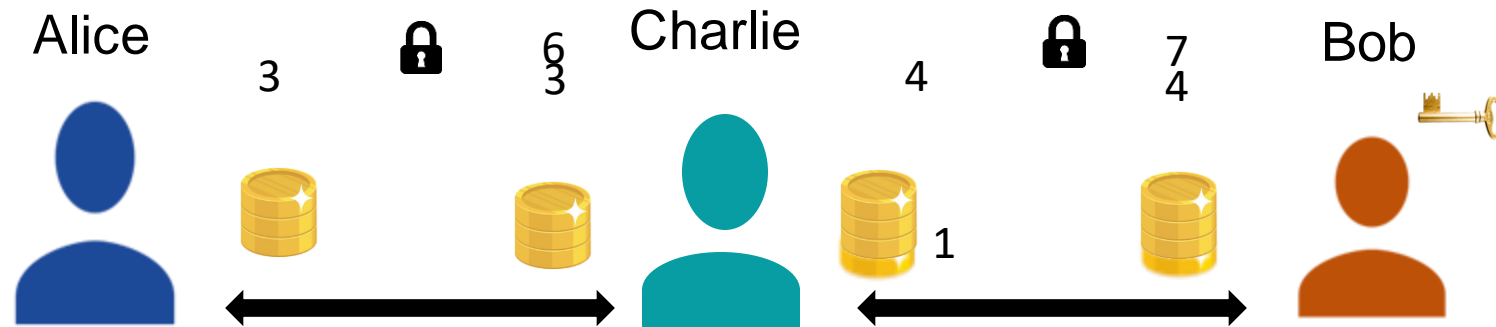
Credit Networks

Networks enabling transfer of money, goods, or services through trust lines



Payment Channel Networks

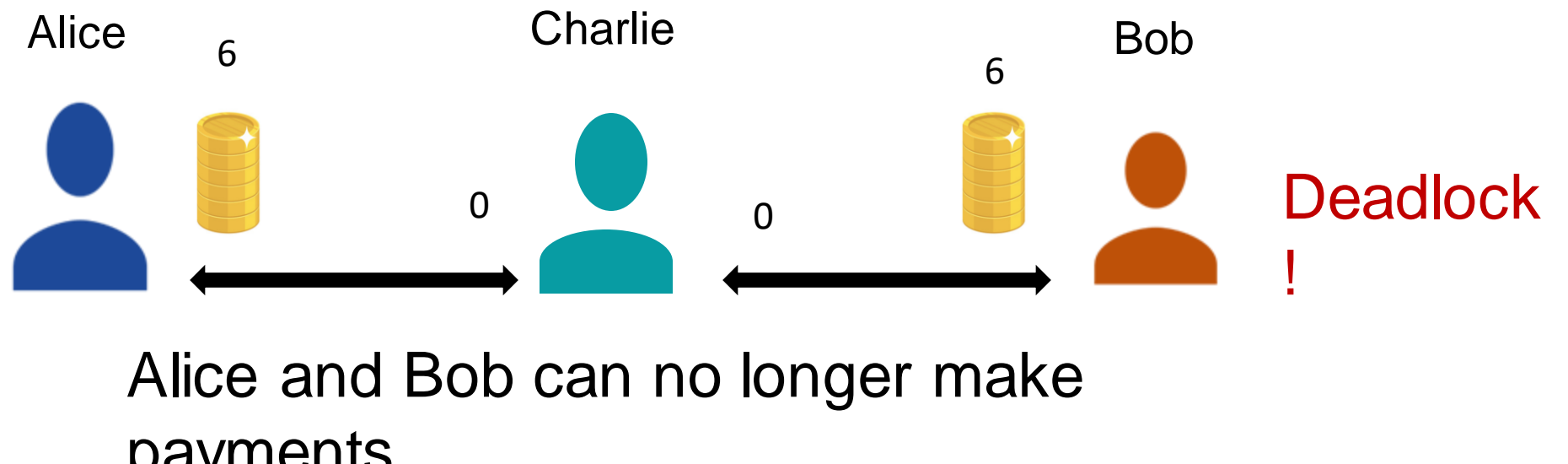
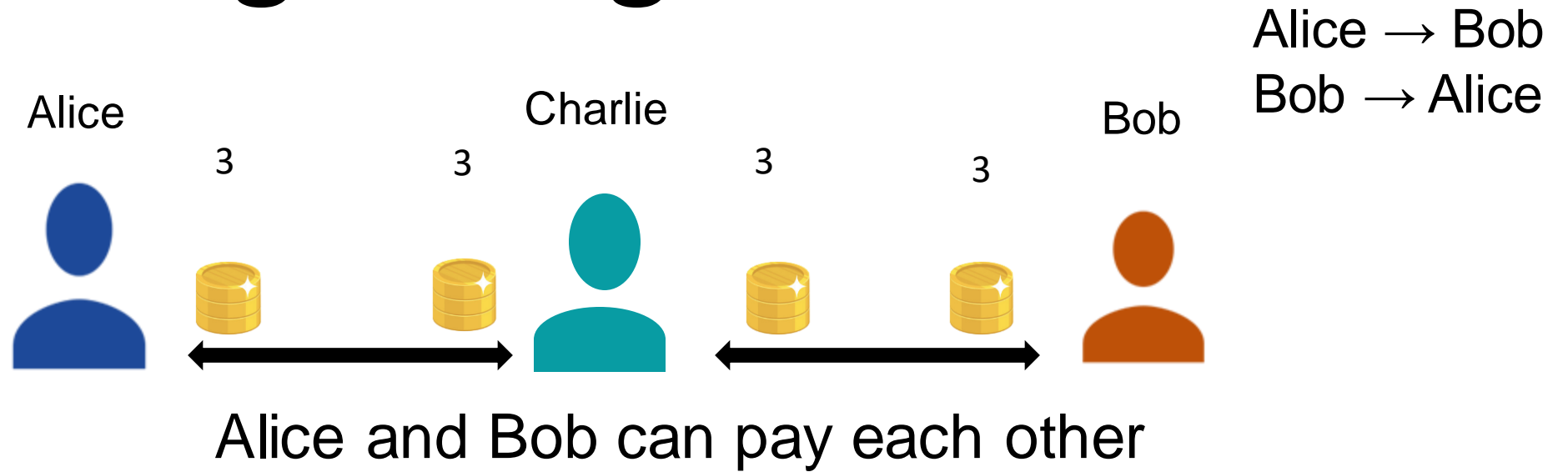
Alice wants to send
3 coins to Bob



Alice can no longer pay Bob

How does the configuration affect credit network throughput?

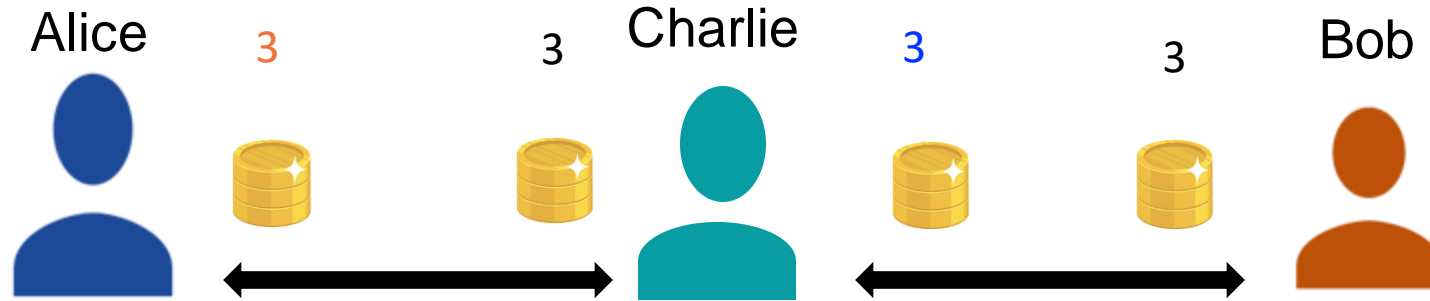
Comparing Configurations



Simplified Model

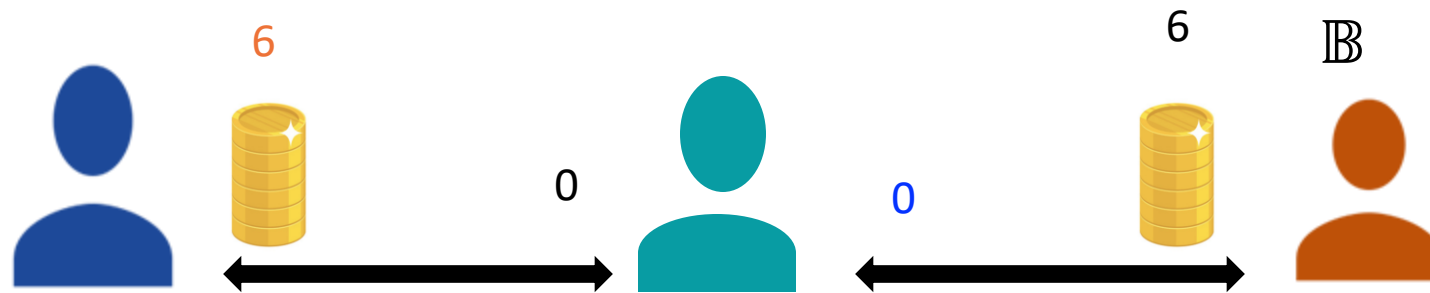
$G(E, V)$

$$b = \begin{bmatrix} 3 \\ 3 \end{bmatrix}$$



$$\text{Capacity} = \begin{bmatrix} 6 \\ 6 \end{bmatrix}$$

$$b = \begin{bmatrix} 6 \\ 0 \end{bmatrix}$$



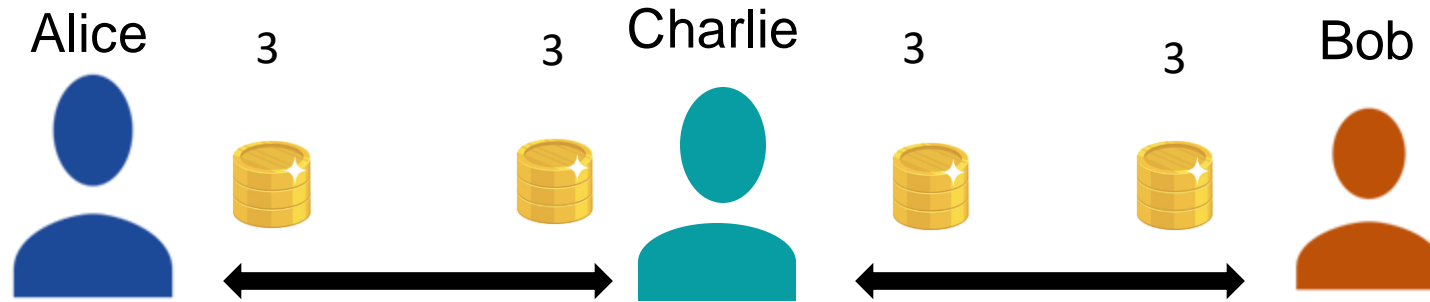
Balance State Space \mathbb{B}

Demand D:
Alice \rightarrow Bob
Bob \rightarrow Alice

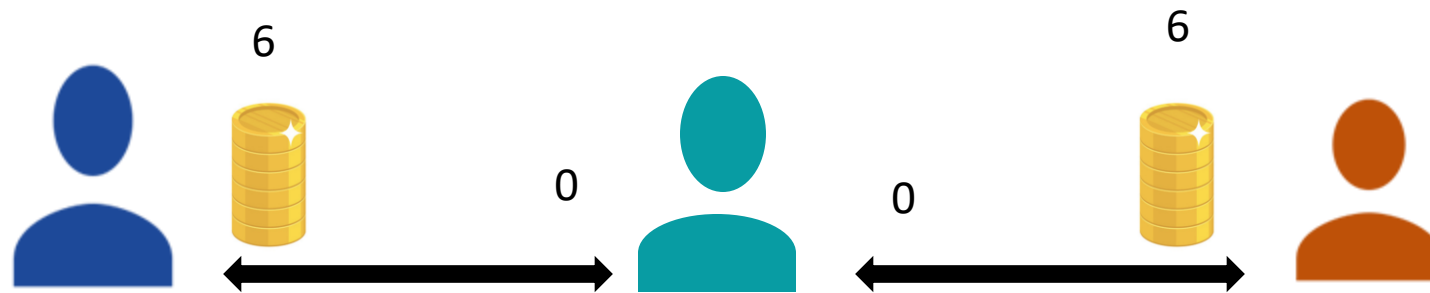
Steady-state Throughput $\phi(b) =$

$$\lim_{T \rightarrow \infty} \frac{\sum_{t=0}^T \text{Throughput}(t)}{T}$$
 (Subject to Demand D and topology)

Throughput Sensitivity



$$\phi_{\max} = \max_{b \in \mathbb{B}} \phi(b) = 6$$



$$\phi_{\min} = \min_{b \in \mathbb{B}} \phi(b) = 0$$

$$\phi_{\min} \neq \phi_{\max}$$

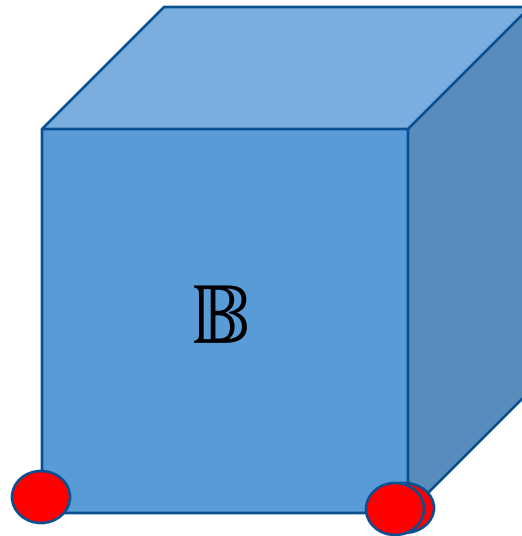
When is $\phi_{\min} \approx \phi_{\max}$?

Throughput Sensitivity

Throughput Inequality

Deadlocks and Throughput Sensitivity

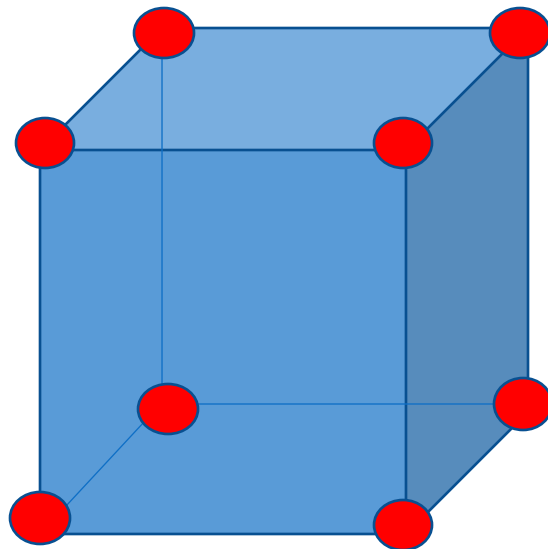
Theorem 1: No deadlocks \Rightarrow Throughput Insensitivity



Deadlocks and Throughput Sensitivity

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Theorem 2: Minimum throughput ϕ_{\min} achieved at state with most deadlocked channels



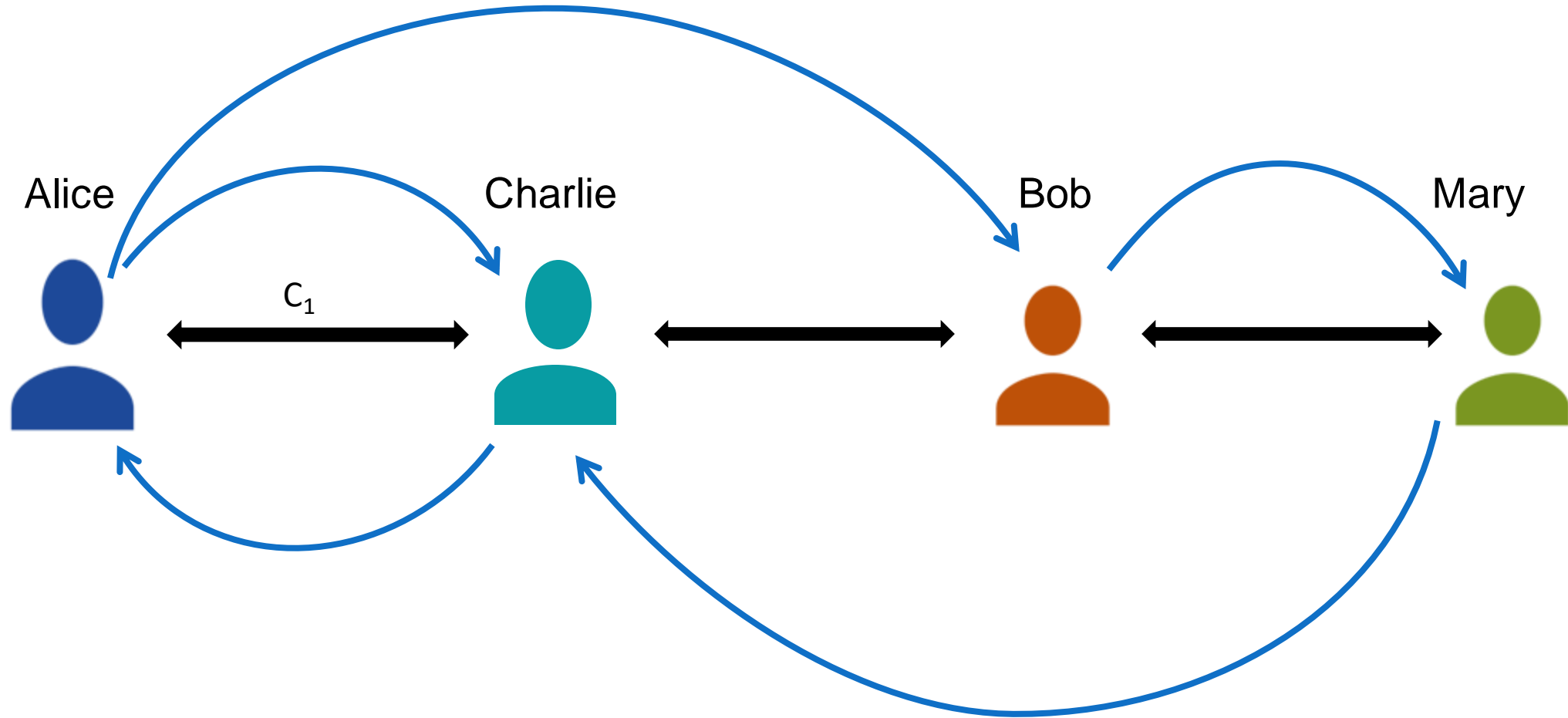
Deadlocks and Throughput Sensitivity

Theorem 1: No deadlocks \Rightarrow Throughput Insensitivity

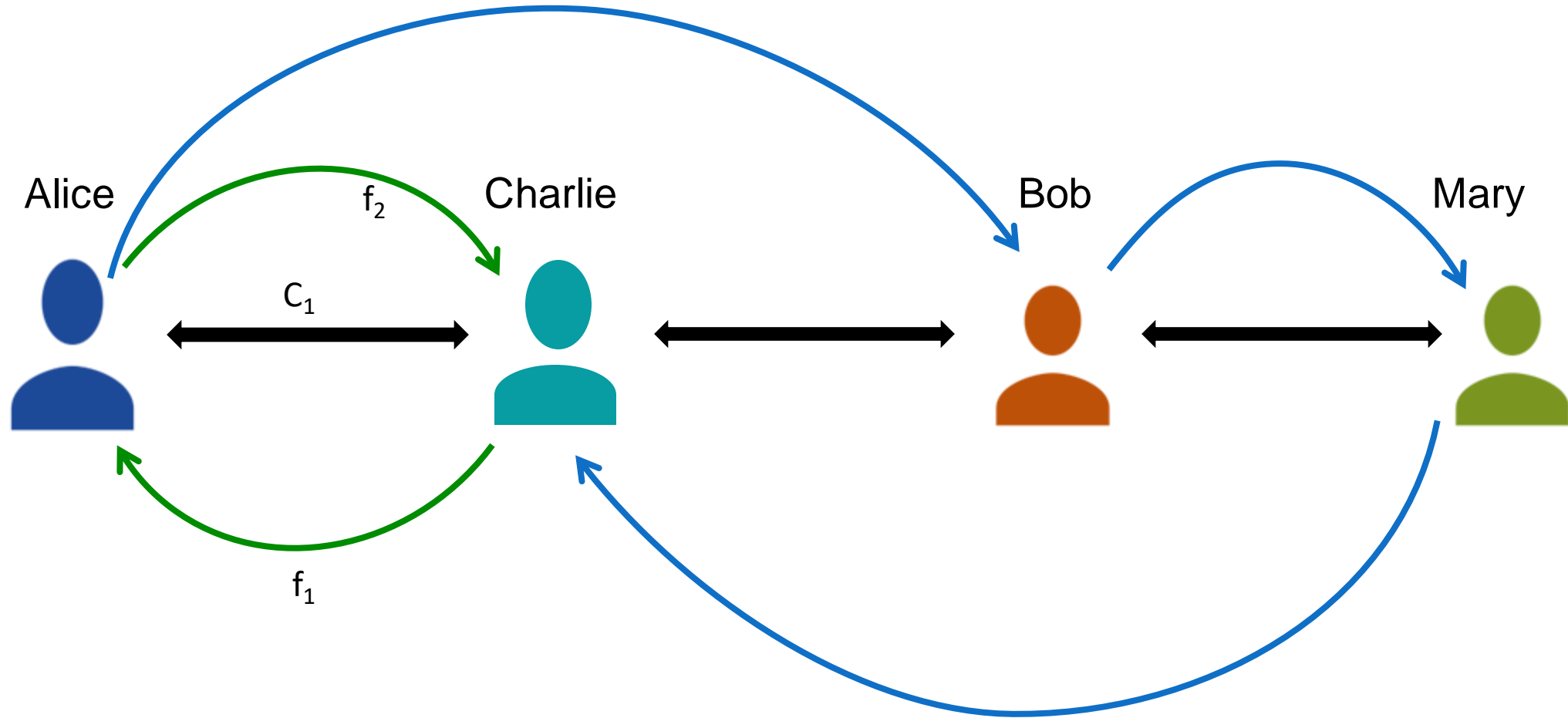
Theorem 2: Minimum throughput ϕ_{\min} achieved at state with most deadlocked channels

Theorem 3: Deadlock detection is NP-Hard

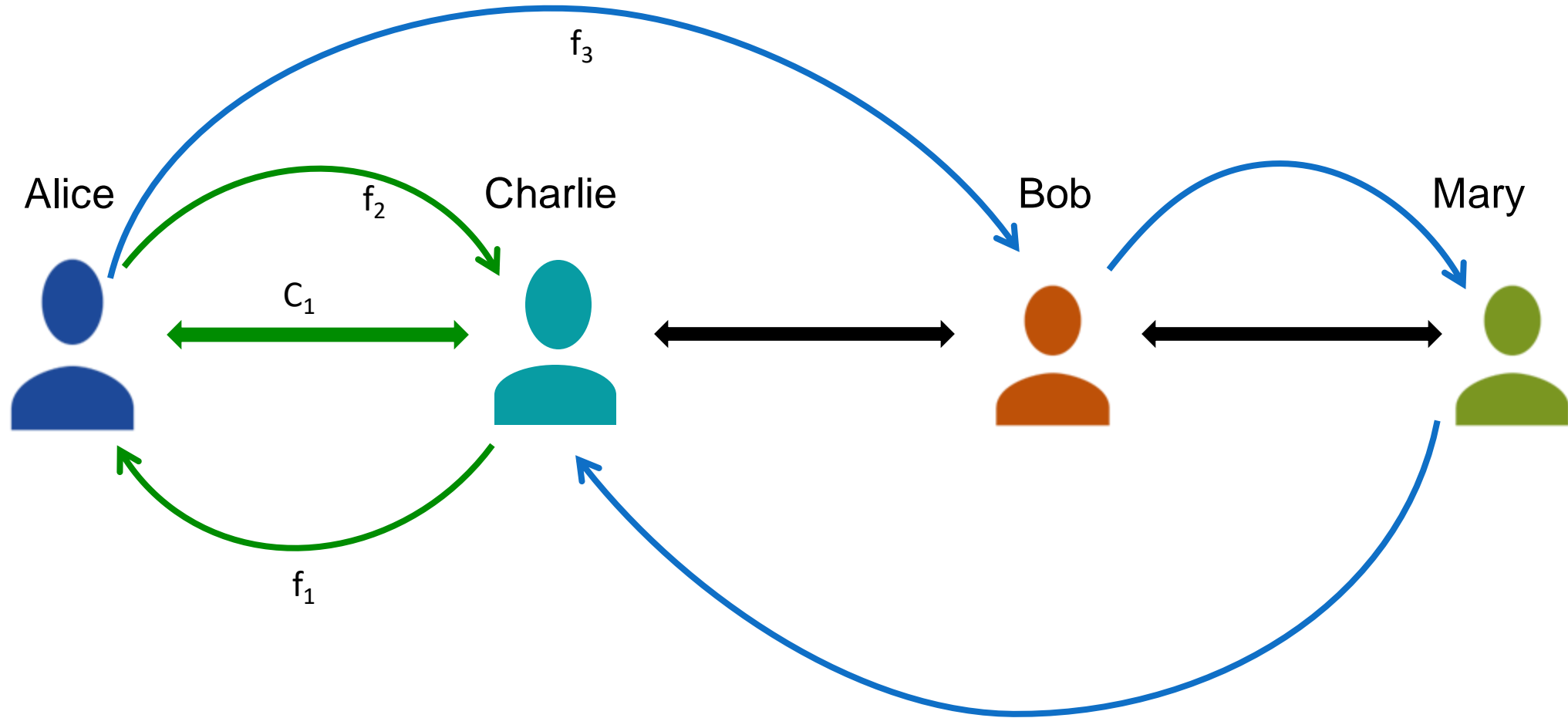
Detecting Deadlocks



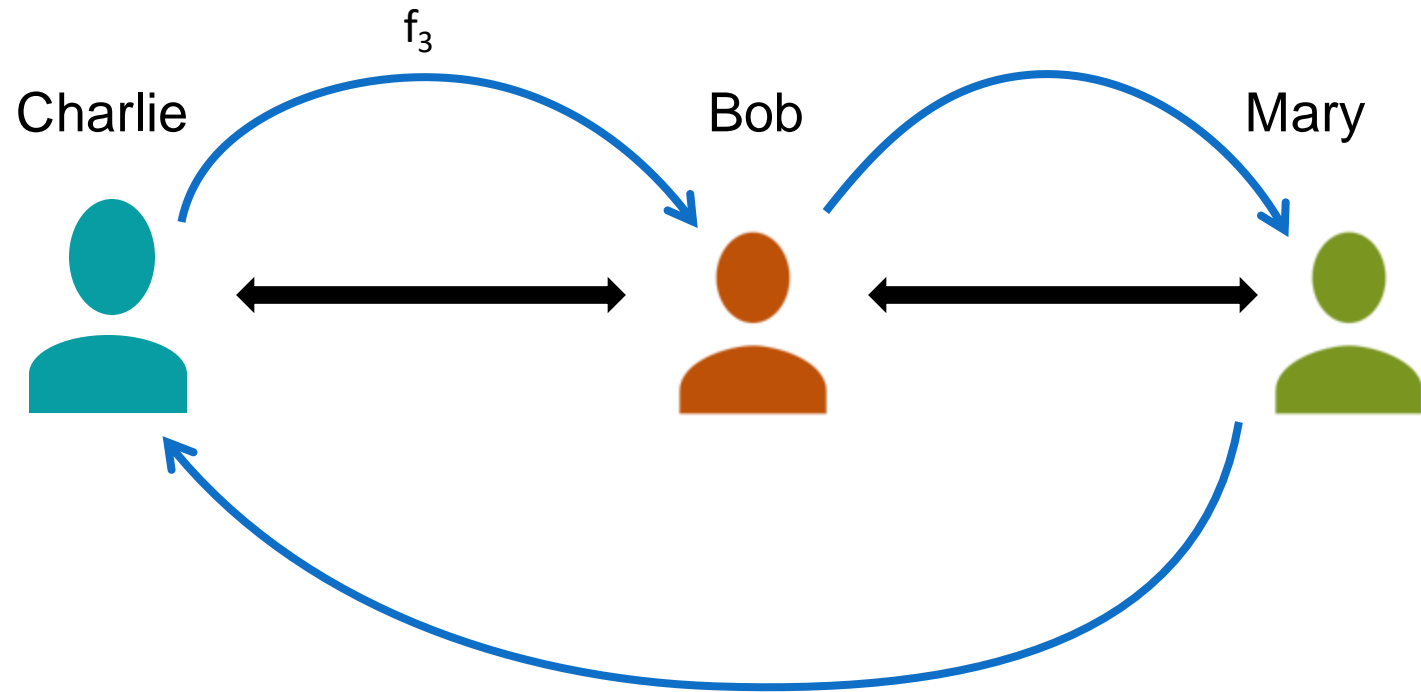
Detecting Deadlocks



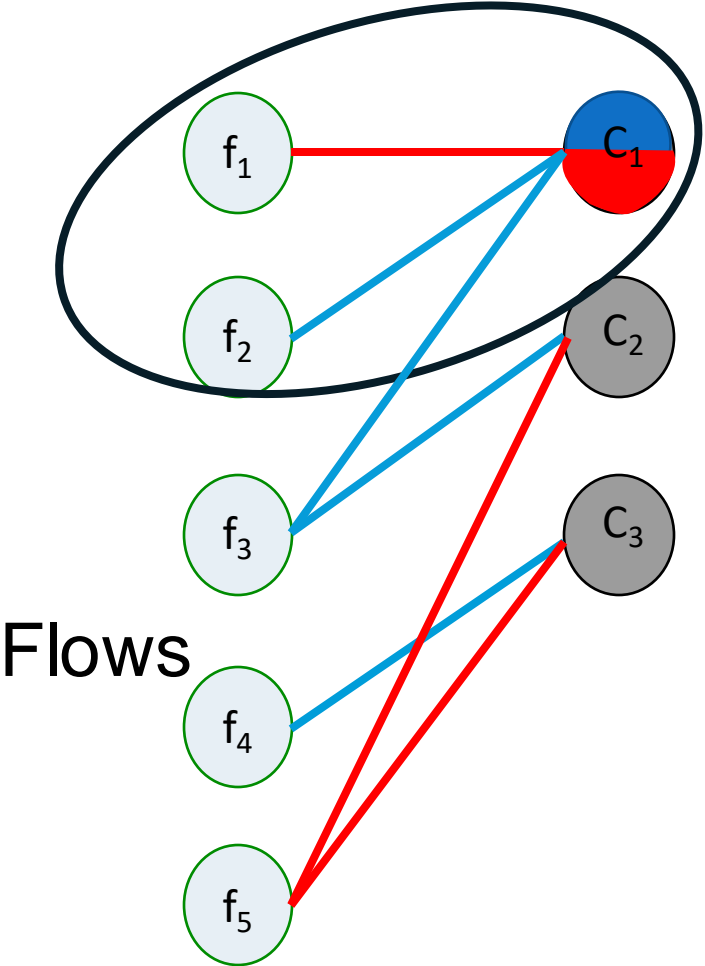
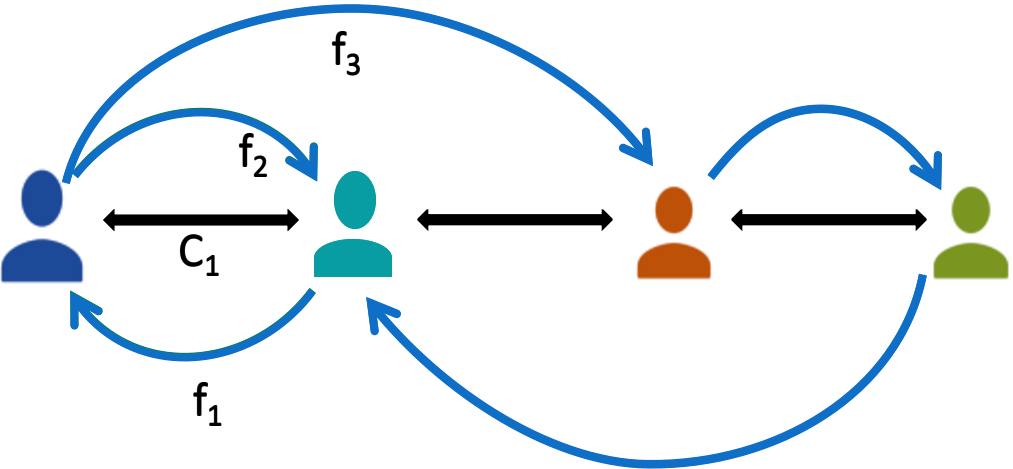
Detecting Deadlocks



Detecting Deadlocks



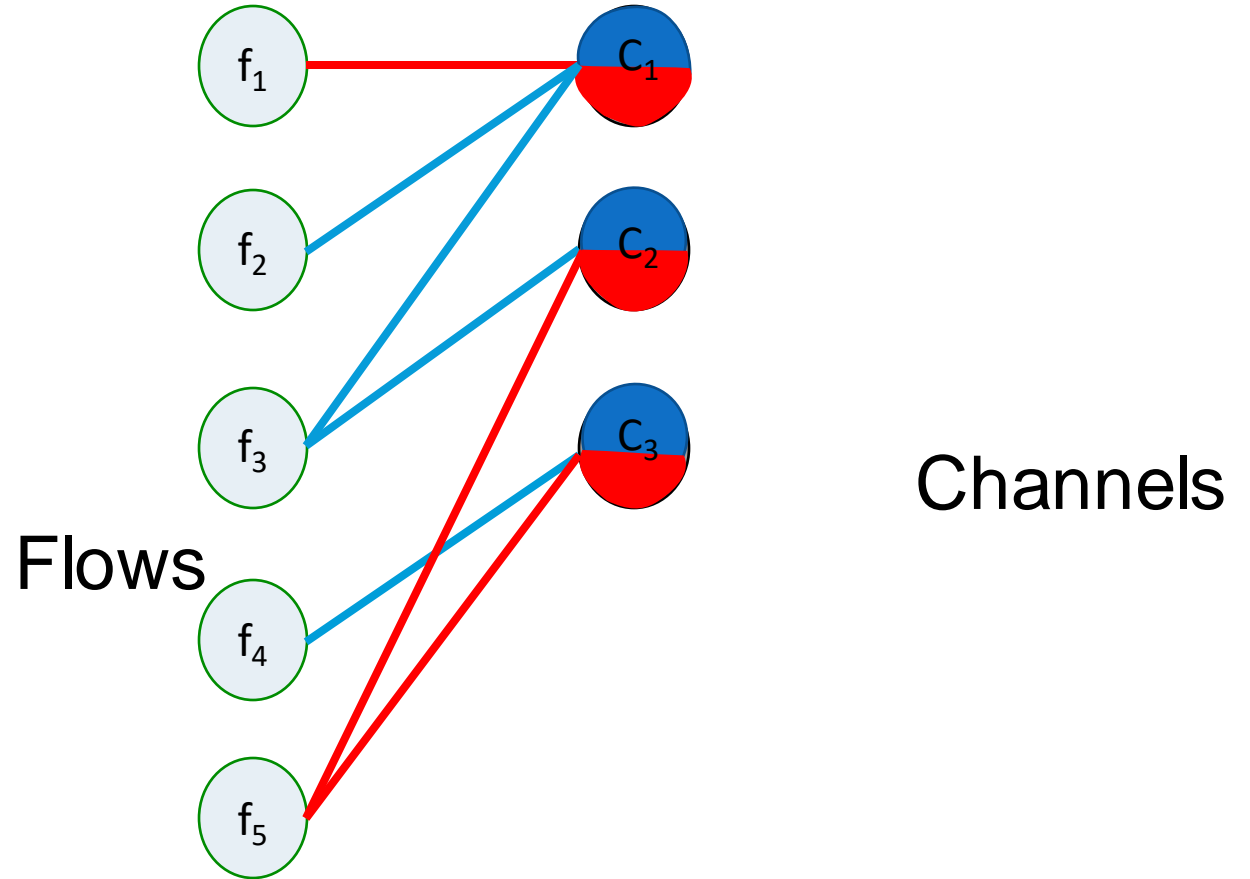
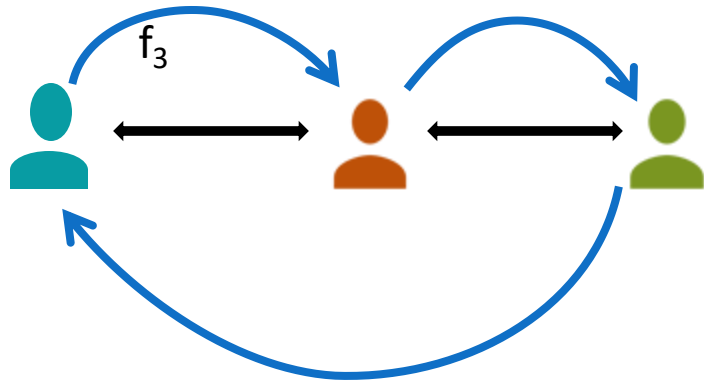
Deadlock Peeling Algorithm



Channels

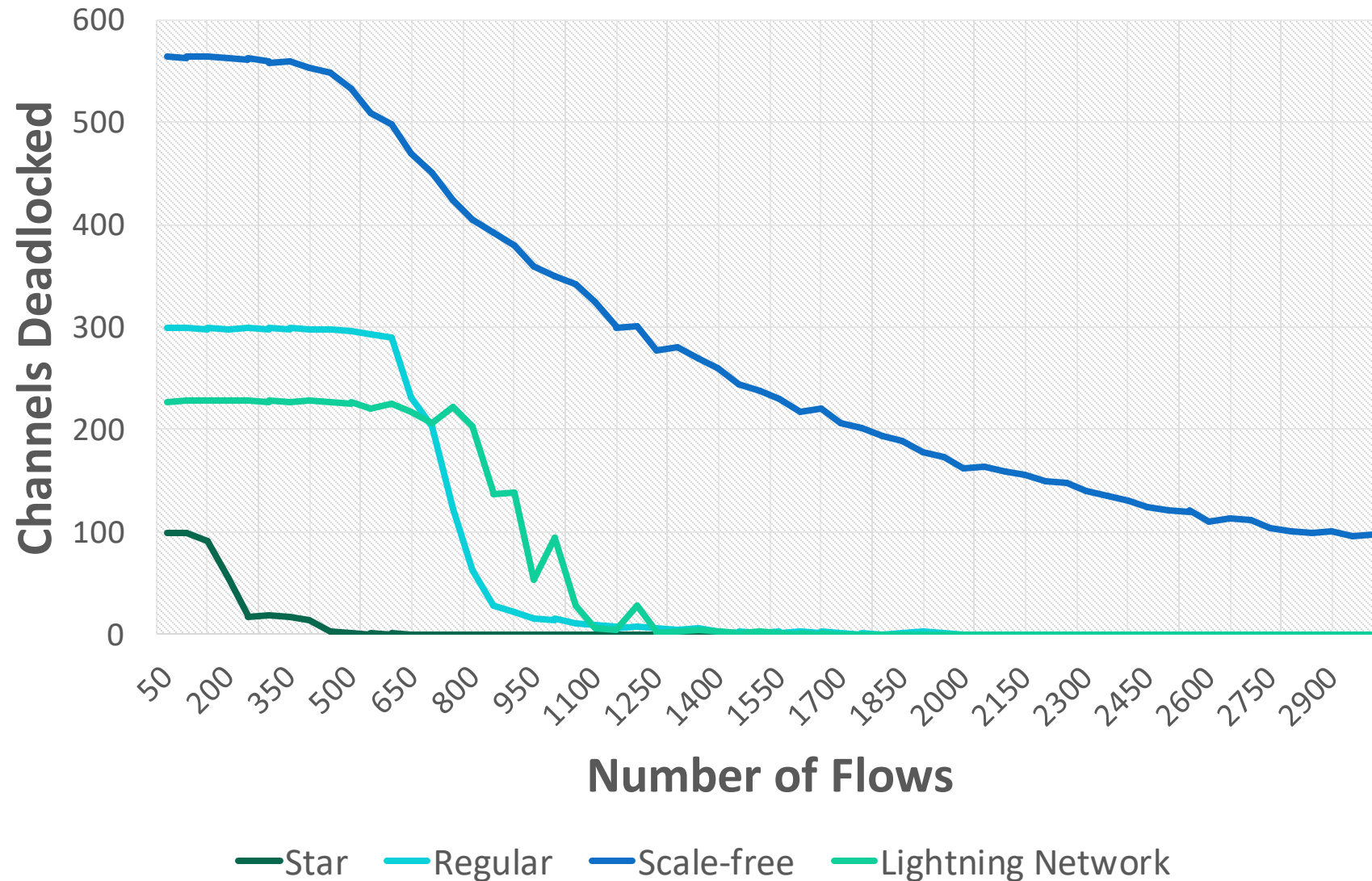
Flows

Deadlock Peeling Algorithm

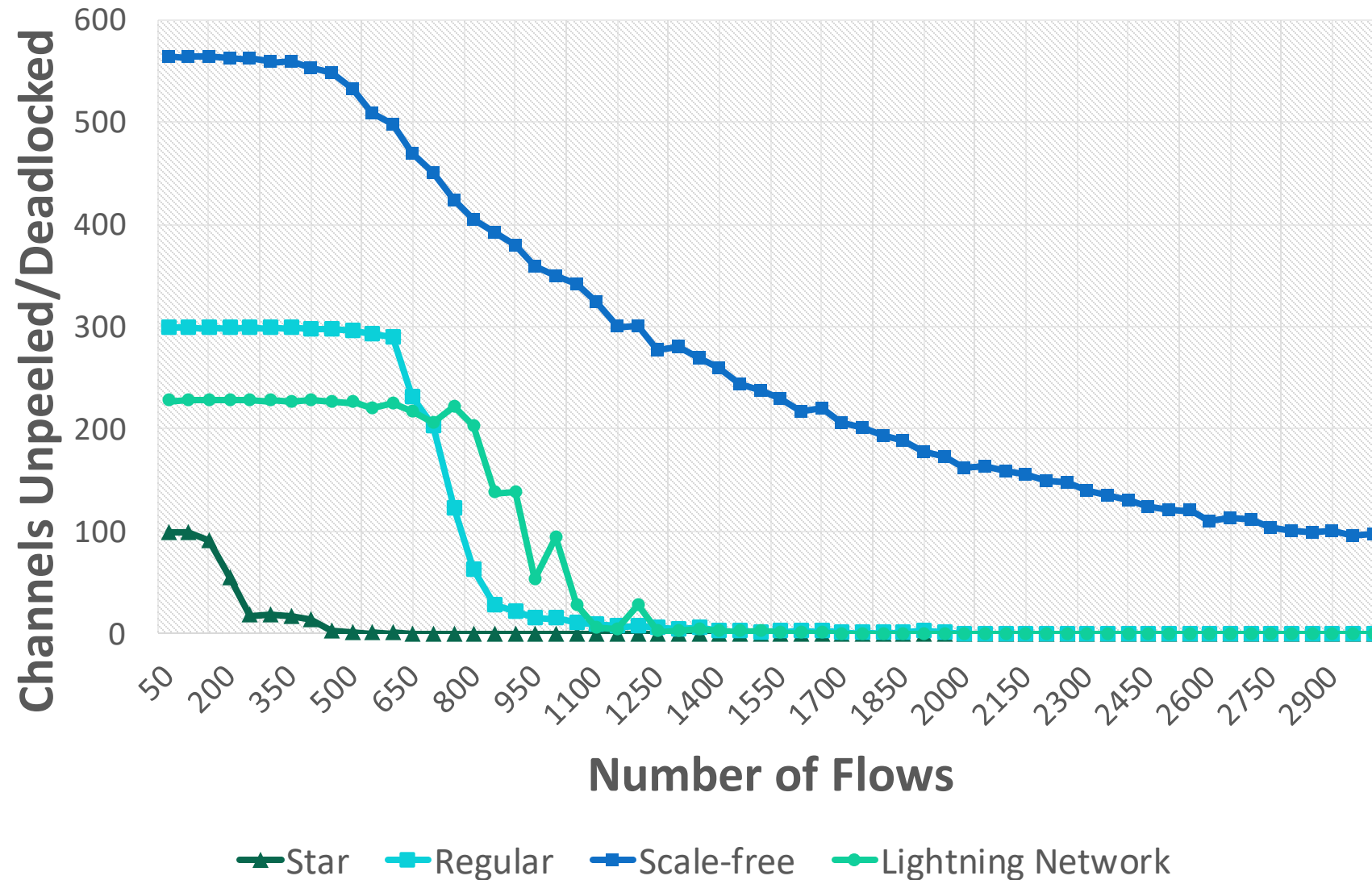


Termination depends on path length distribution

Peeling Algorithm Accuracy



Peeling Algorithm Accuracy



Topology Synthesis

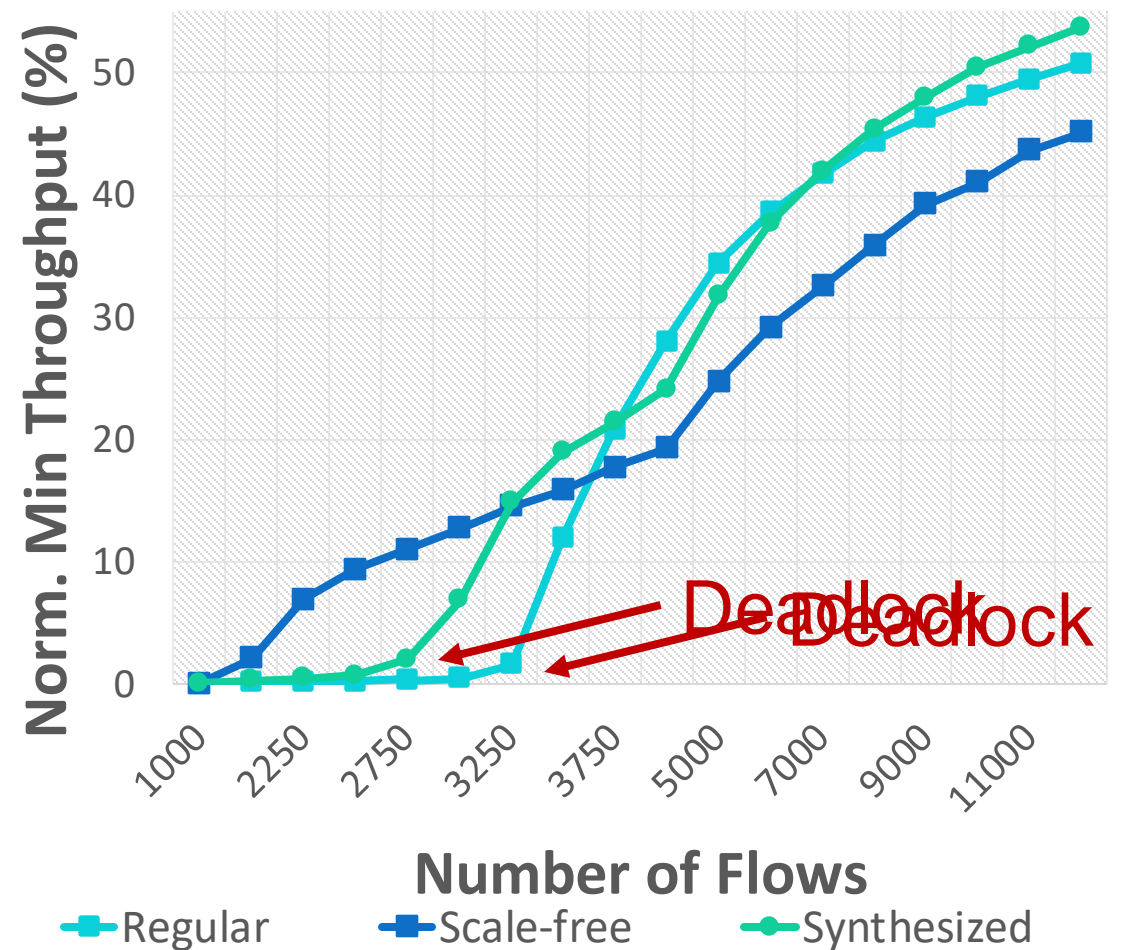
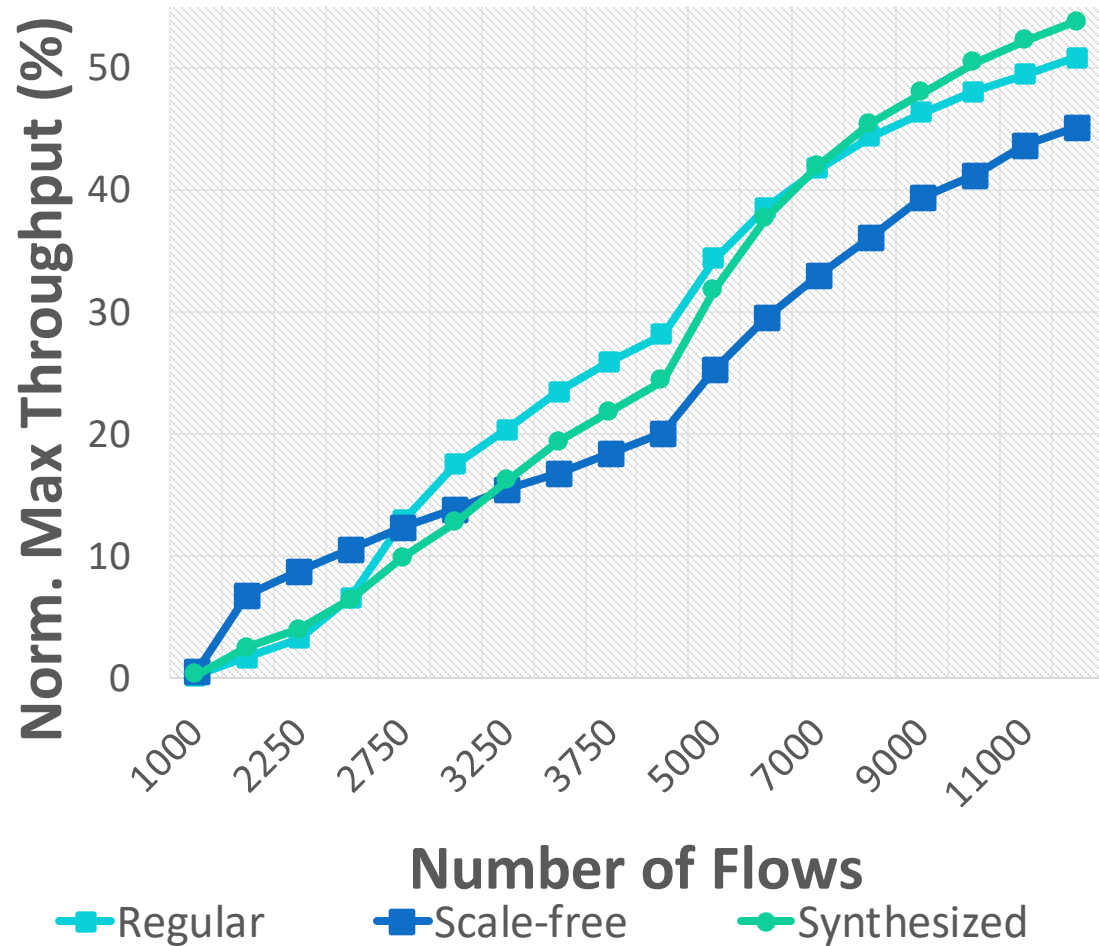
Peeling algorithm finds deadlock-free channels and helps compute ϕ_{\min}

Synthesize robust topologies with good peeling behavior

Insight: Termination depends on path length distribution

Leverage peer-recommendation services such as “autopilot”

Topology Synthesis



Summary

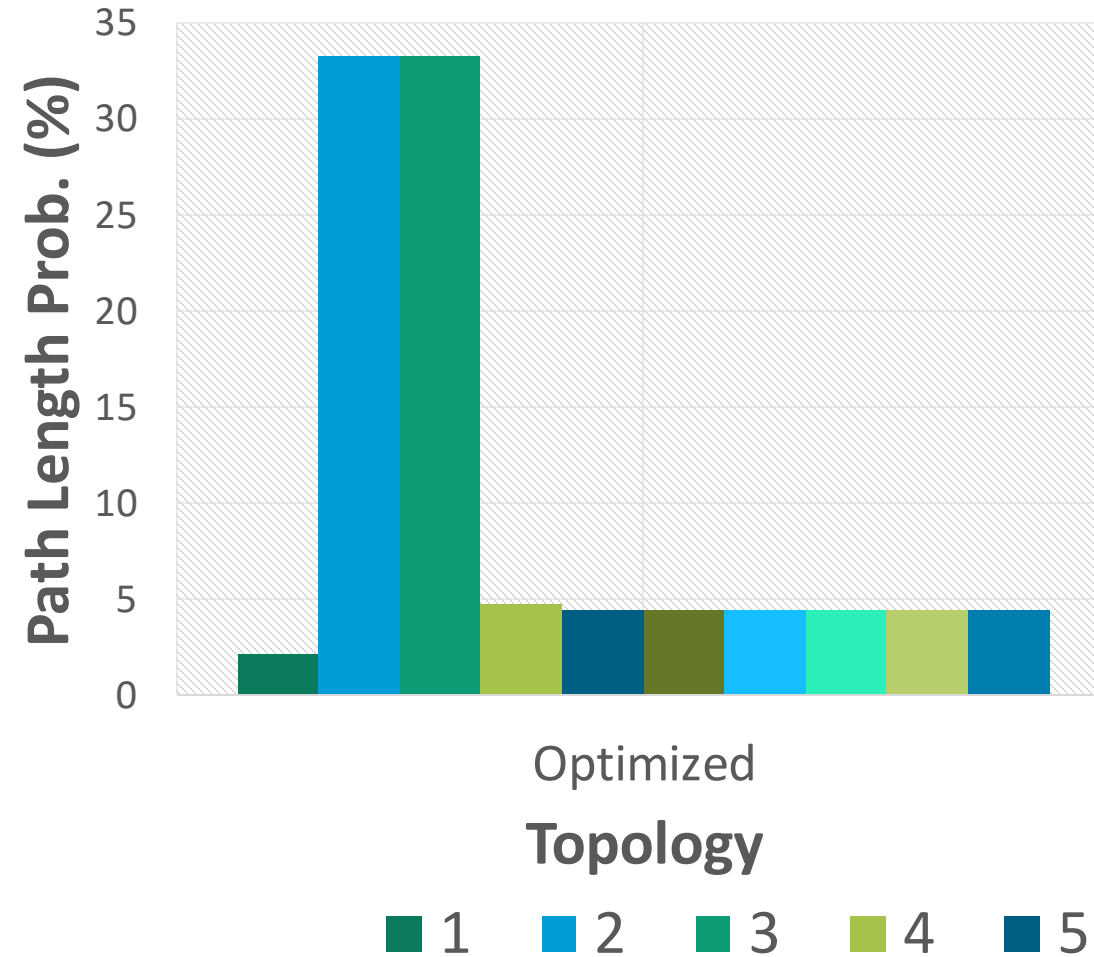
Credit networks enable money transfer through trust relationships

Potential for imbalance and deadlocks can cause discrepancies in throughput based on the starting configuration

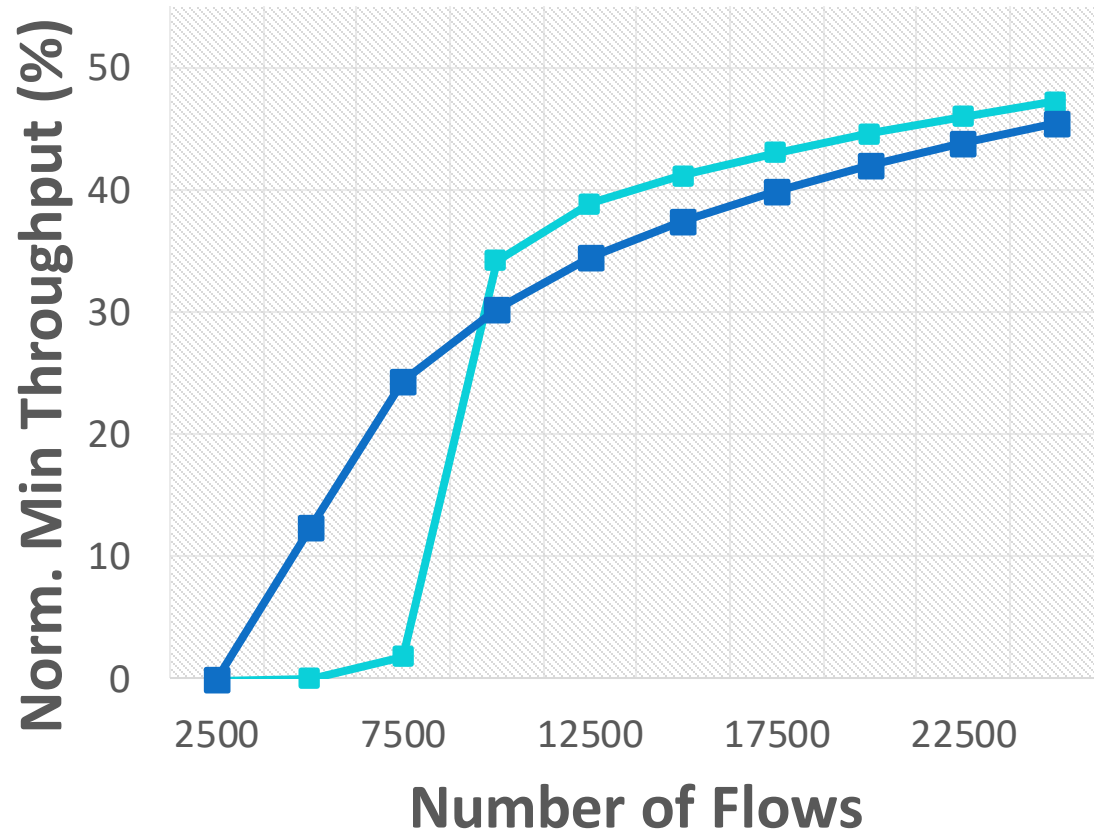
Topology synthesis techniques can further improve the worst-case throughput behavior

Contact: vibhaa@mit.edu

Optimized Distribution

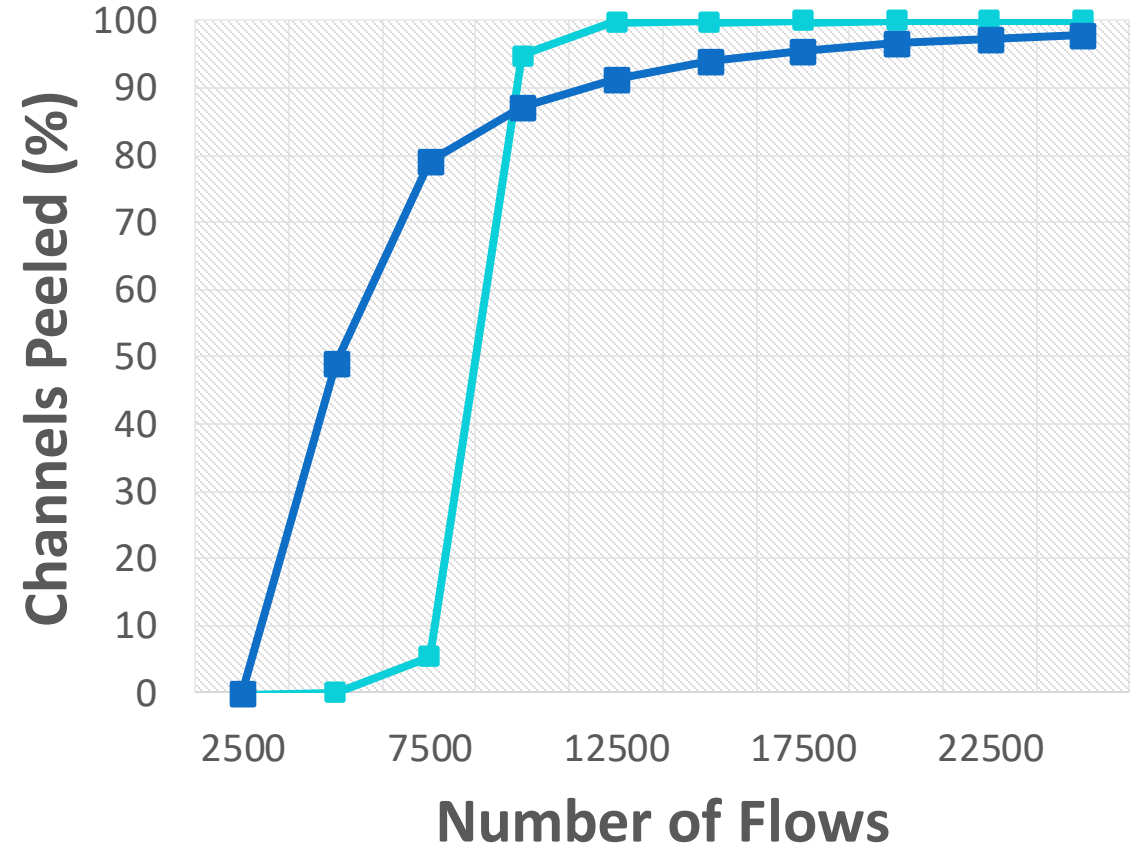


Topology Comparison



Regular

Scale-free



Regular

Scale-free

Topology Comparison

